

# Porte Universali

## Architettura degli Elaboratori e Laboratorio

14 Marzo 2013

# Proprietá dell'algebra di Boole

Identità:

$$A + 0 = A$$

$$A \cdot 1 = A$$

Nullo:

$$A + 1 = 1$$

$$A \cdot 0 = 0$$

Idempotente:

$$A + A = A$$

$$A \cdot A = A$$

Inverso:

$$A + \bar{A} = 1$$

$$A \cdot \bar{A} = 0$$

Commutativa:

$$A + B = B + A$$

$$A \cdot B = B \cdot A$$

Associativa:

$$A + (B + C) = (A + B) + C$$

$$A \cdot (B \cdot C) = (A \cdot B) \cdot C$$

Distributiva:

$$A \cdot (B + C) = (A \cdot B) + (A \cdot C)$$

$$A + (B \cdot C) = (A + B) \cdot (A + C)$$

DeMorgan:

$$\overline{A + B} = \bar{A} \cdot \bar{B}$$

$$\overline{A \cdot B} = \bar{A} + \bar{B}$$

# Porte Logiche

NOT

$A$	$O$
0	1
1	0

AND

$A$	$B$	$O$
0	0	0
0	1	0
1	0	0
1	1	1

NAND

$A$	$B$	$O$
0	0	1
0	1	1
1	0	1
1	1	0

OR

$A$	$B$	$O$
0	0	0
0	1	1
1	0	1
1	1	1

NOR

$A$	$B$	$O$
0	0	1
0	1	0
1	0	0
1	1	0

XOR

$A$	$B$	$O$
0	0	0
0	1	1
1	0	1
1	1	0

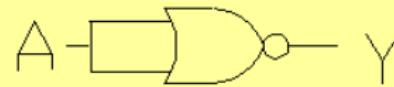
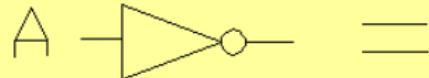
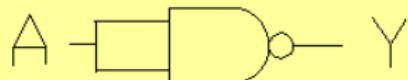
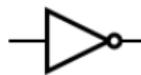


# Porte Logiche Universali NAND e NOR

Tutti i circuiti digitali possono essere espressi utilizzando solo porte NAND o NOR dato che tutte le porte logiche fondamentali sono esprimibili in funzione di queste due.

NOT

A	O
0	1
1	0

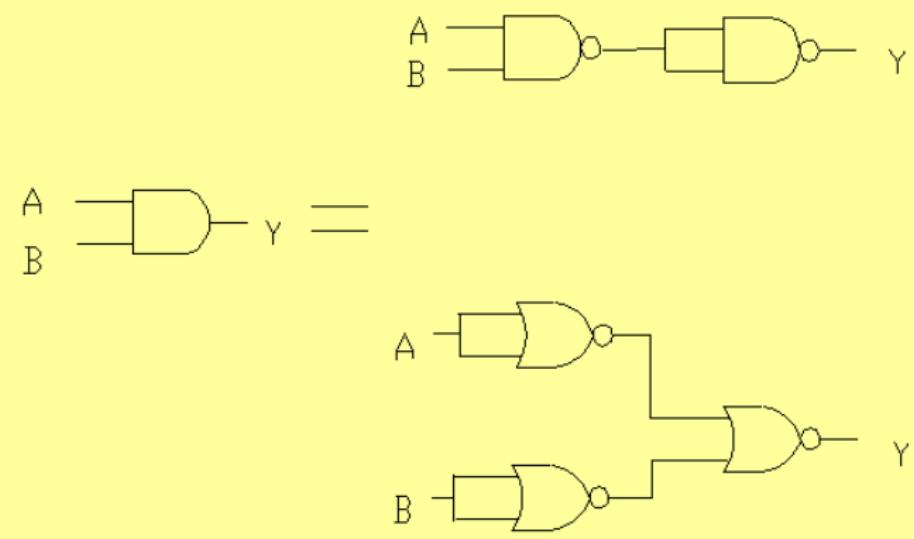


$$\bar{A} = \overline{A \cdot A} = \overline{A + A}$$

# Porte Logiche Universali NAND e NOR

AND

A	B	O
0	0	0
0	1	0
1	0	0
1	1	1

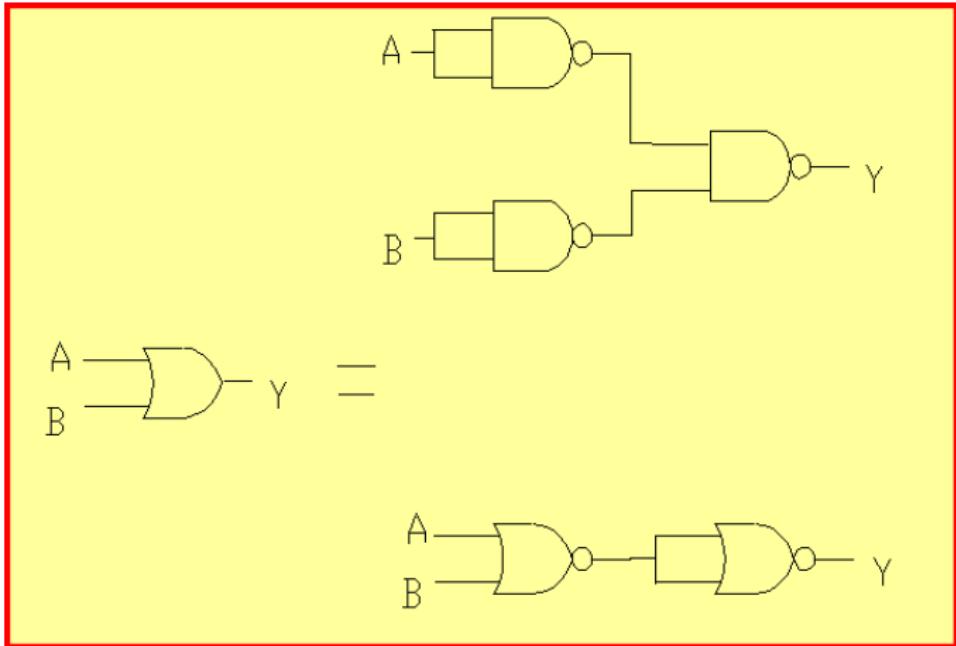


$$A \cdot B = \overline{\overline{A} \cdot \overline{B}} = \overline{\overline{A} + \overline{B}}$$

# Porte Logiche Universali NAND e NOR

OR

A	B	O
0	0	0
0	1	1
1	0	1
1	1	1

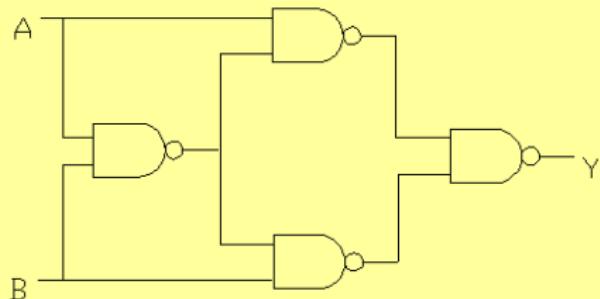
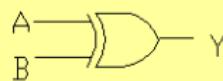


$$A + B = \overline{\overline{A} \cdot \overline{B}} = \overline{\overline{A} + \overline{B}}$$

# Porte Logiche Universali NAND e NOR

XOR

A	B	O
0	0	0
0	1	1
1	0	1
1	1	0

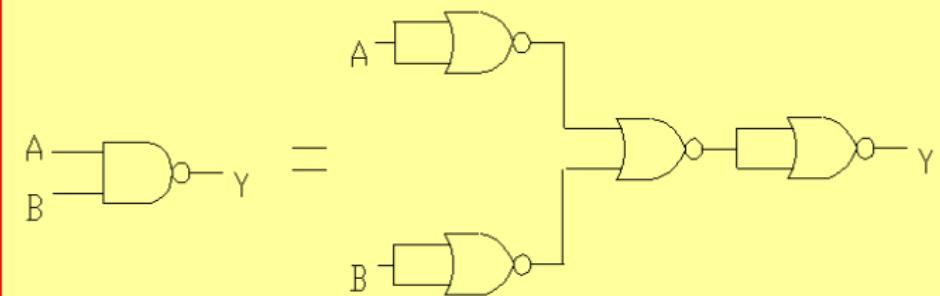


$$\begin{aligned}
 \overline{A} \cdot B + A \cdot \overline{B} &= \overline{\overline{A} \cdot \overline{A}} \cdot B \cdot \overline{A \cdot \overline{B} \cdot B} = \overline{\overline{A} \cdot \overline{A}} \cdot \overline{B} \cdot \overline{B} \cdot \overline{A} \cdot \overline{B} = \\
 \overline{\overline{A} + \overline{A} + \overline{B} + \overline{B}} + \overline{A + B} &= \overline{A + A + B + B} + \overline{B + A + B} = A + A + \overline{B} + B + A + B
 \end{aligned}$$

## Porte Logiche Universali NAND e NOR

NAND

A	B	O
0	0	1
0	1	1
1	0	1
1	1	0

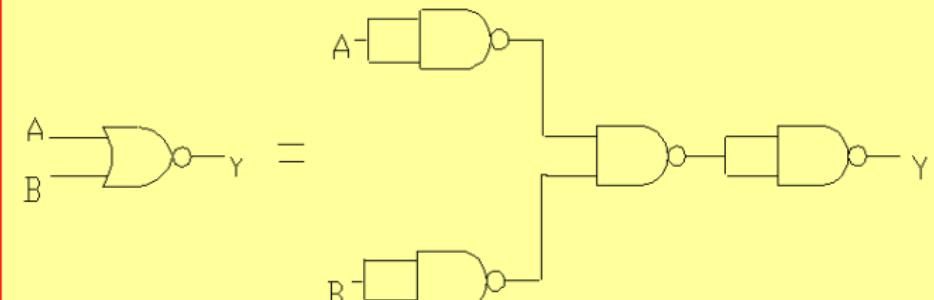


$$\overline{A \cdot B} = \overline{\overline{A} + \overline{B}}$$

## Porte Logiche Universali NAND e NOR

NOR

A	B	O
0	0	0
0	1	1
1	0	1
1	1	1



$$\overline{A + B} = \overline{\overline{A} \cdot \overline{B}}$$