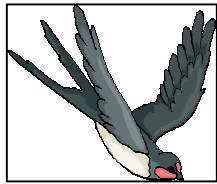


5th Forum on New Materials, Materials Solutions for Sustainable Energy, Montecatini Terme (PT), June 13-18, 2010



# Optical Methods for Indoor Characterization of Small Size Solar Concentrators

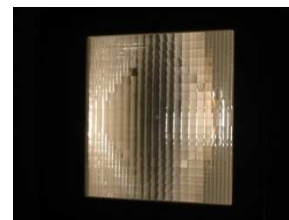


University of Ferrara  
Department of Physics

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D. Uderzo<sup>3</sup>, Paolo Zurru<sup>3</sup>, Giuliano Martinelli<sup>2</sup>



<sup>1</sup>ENEA Centro Ricerche "E. Clementel", Bologna, Italy  
<sup>2</sup>Università di Ferrara, Dipartimento di Fisica, Ferrara, Italy  
<sup>3</sup>CPower srl, Ferrara, Italy.





***Reverse the sight of your world  
You will get surprises!***

# SUMMARY

Short introduction to *nonimaging* solar concentrators

“**Direct methods**” of characterization of concentrators

- i) The direct laser method (DLM)
- ii) The direct collimated method (DCM)
- iii) The direct integral method (DIM)

The “**Inverse method**” (IM) of characterization of concentrators

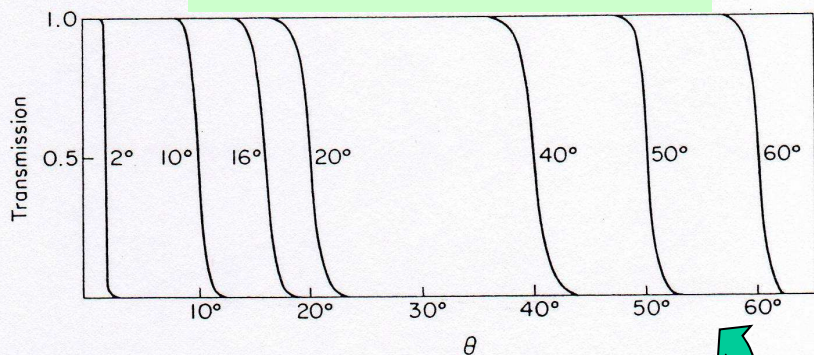
Applications

- \* Ideal 3D-CPCs
- \* Truncated and Squared CPCs
- \* Fresnel and prismatic lenses
- \* The “**Rondine**<sup>®</sup>” nonimaging PV concentrator

Conclusions

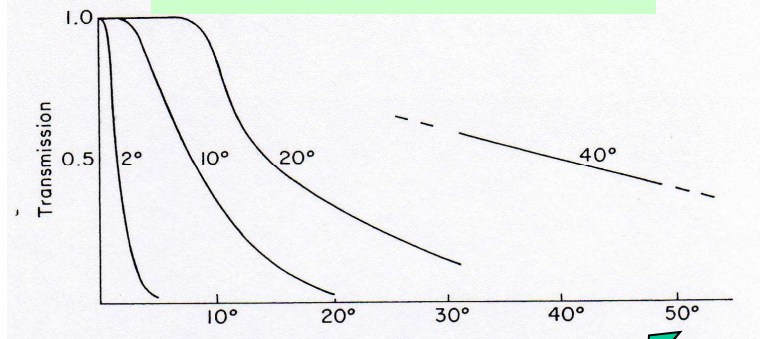
# Optical efficiency curves of 3D-concentrators

3D-CPC Solar concentrator

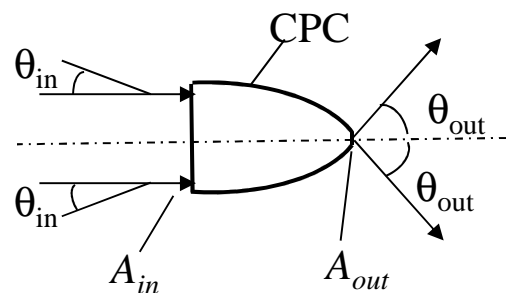


NONIMAGING

3D Parabolic concentrator

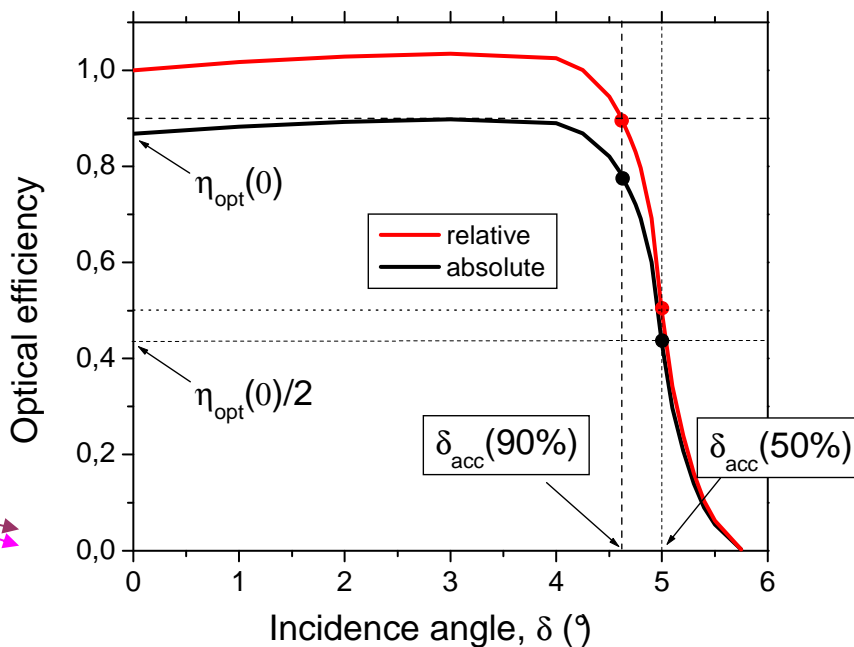
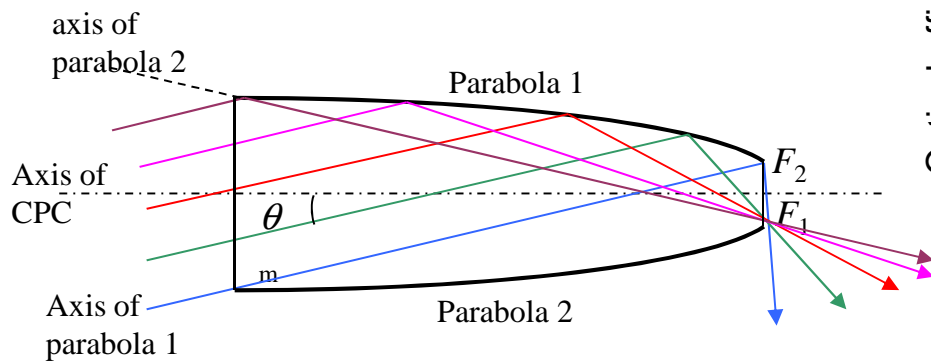


IMAGING



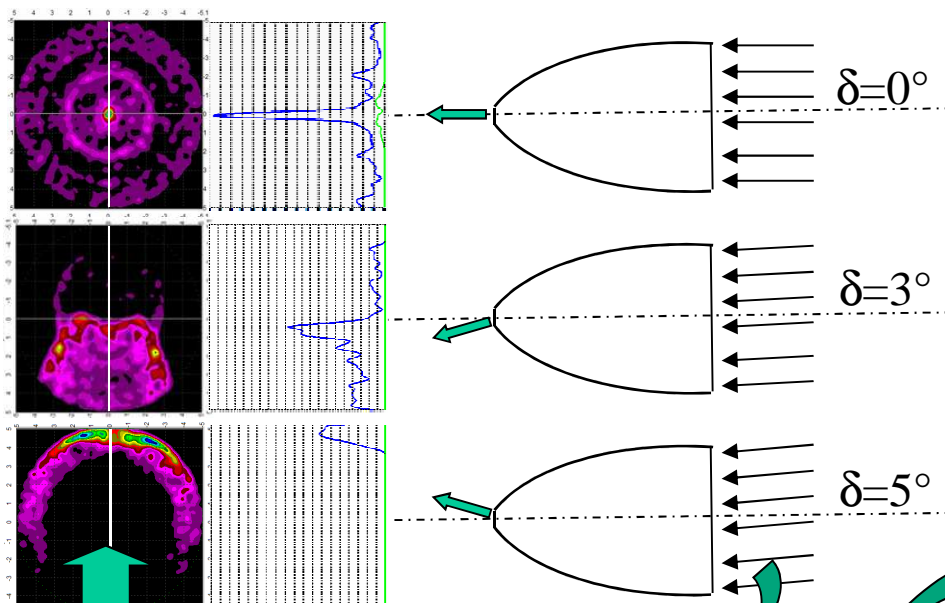
$$C_{opt} = \frac{\sin^2 \theta_{out}}{\sin^2 \theta_{in}}$$

(in air)

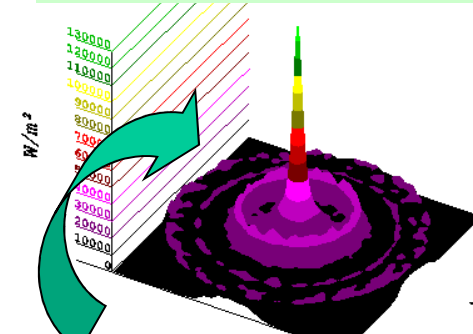


Absolute and relative transmission efficiency curves

# The 3D Compound Parabolic Concentrator (3D-CPC)



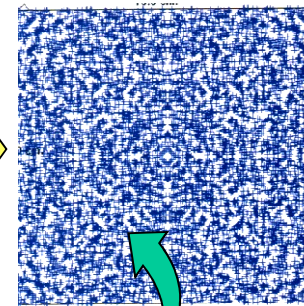
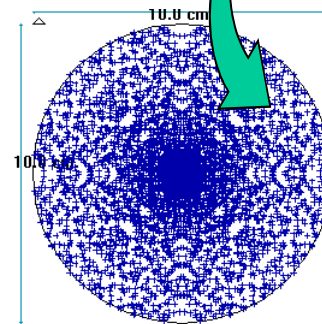
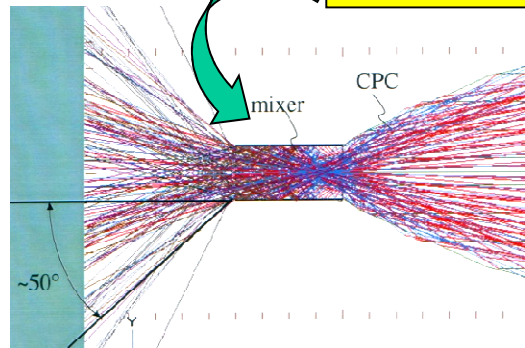
target illumination profile for normal irradiance



In general, we have a non uniform distribution of flux at output

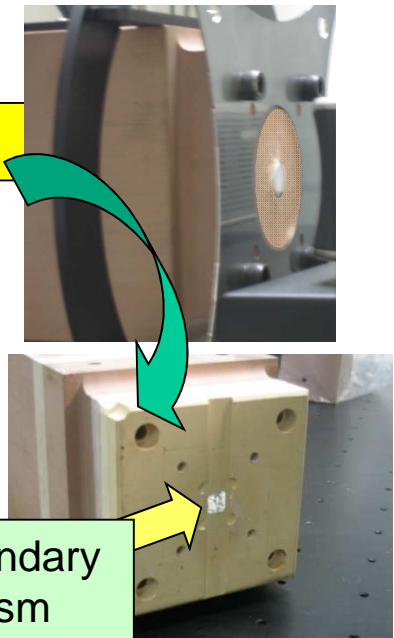
At  $\delta$ =acceptance angle...the flux is on the rim of receiver

But the application of a secondary element...



...allows to obtain a uniform flux at output

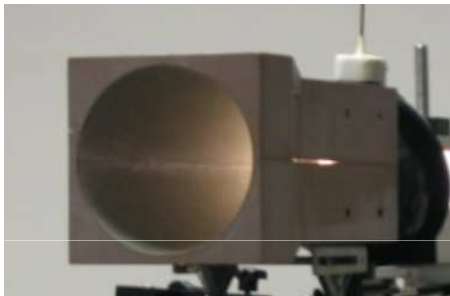
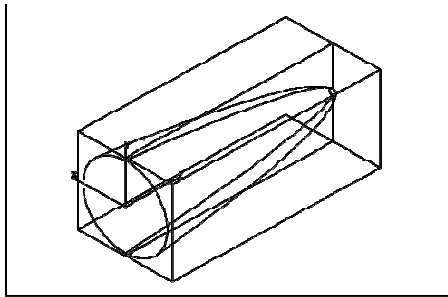
Secondary prism



# THE TESTED SOLAR CONCENTRATORS

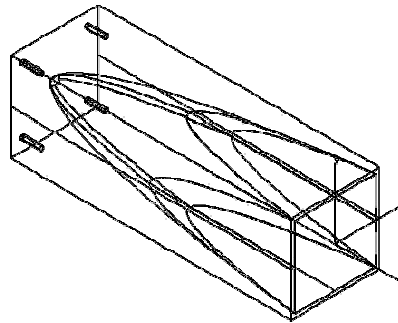
# The solar concentrators

## Nonimaging

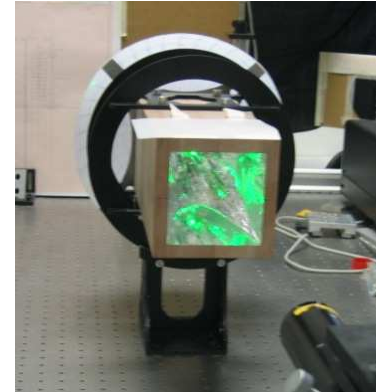


T-CPC  
 $r(\text{in}) = 70 \text{ mm}$   
 $r(\text{out}) = 5 \text{ mm}$   
 $L = 350 \text{ mm}$

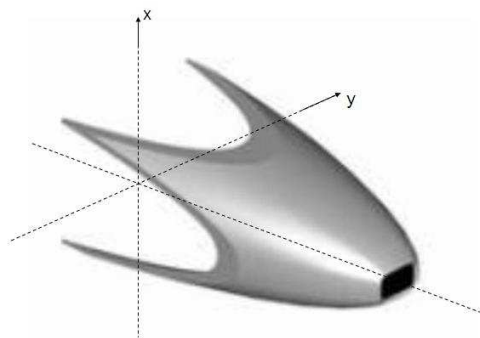
*Truncated CPC (T-CPC)*



TS-CPC  
 $l(\text{in}) = 100 \text{ mm}$   
 $r(\text{out}) = 5 \text{ mm}$   
 $L = 350 \text{ mm}$



## Truncated and Squared CPC (TS-CPC)



$l(\text{in}) = 6,7 \times 6,7 \text{ cm}$   
 $l(\text{out}) = 1,7 \times 1,3 \text{ cm}$   
 $L = 15 \text{ cm}$   
 Axis Tilt =  $6^\circ \times 4^\circ$

*Rondine nonimaging Concentrator (Gen1)*



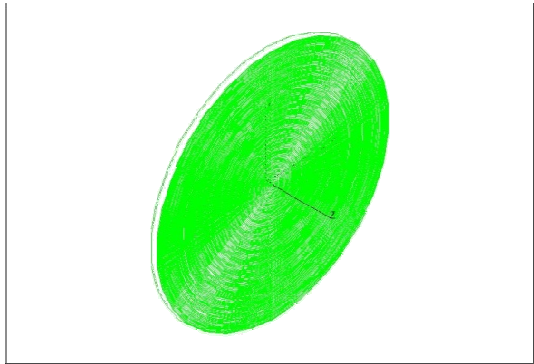
$l(\text{in}) = 3,5 \times 3,5 \text{ cm}$   
 $l(\text{out}) = 0,8 \times 0,8 \text{ cm}$   
 $L = 6.0 \text{ cm}$   
 Axis Tilt =  $5^\circ \times 5^\circ$

*Rondine nonimaging Concentrator (Gen2)*

# The solar concentrators

## *Imaging*

- Fresnel lens (circular):

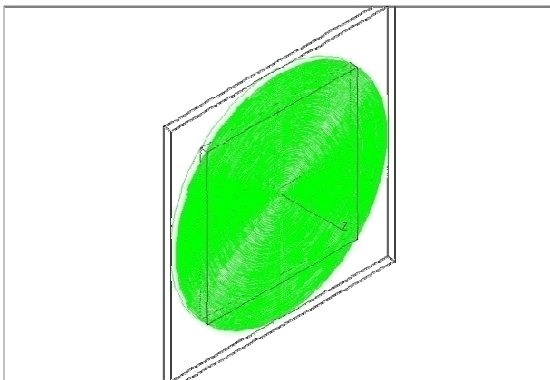


$r=2,8\text{cm}$   
 $d=0,16\text{cm}$



*Prismatic lens Phocus  
concentrator*

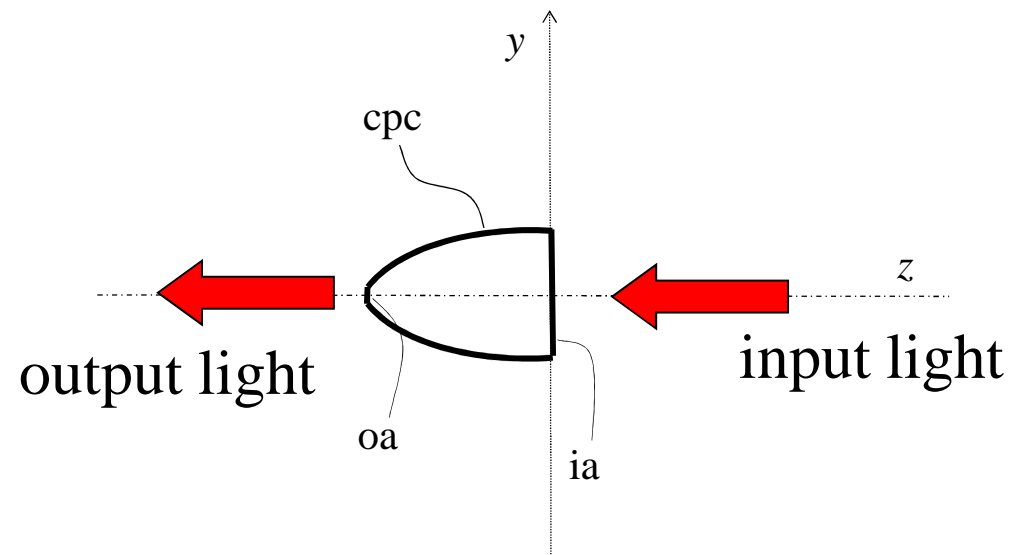
- Fresnel lens (squared):



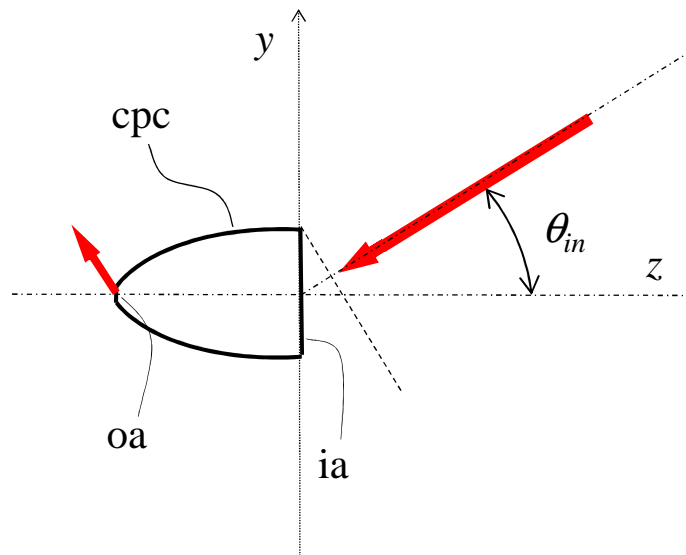
Mask 2x2cm



# THE “DIRECT” METHODS OF CHARACTERIZATION

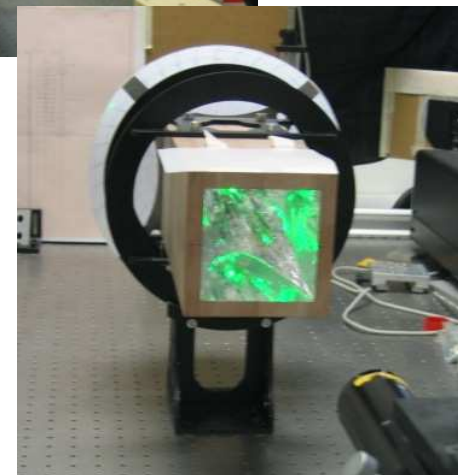
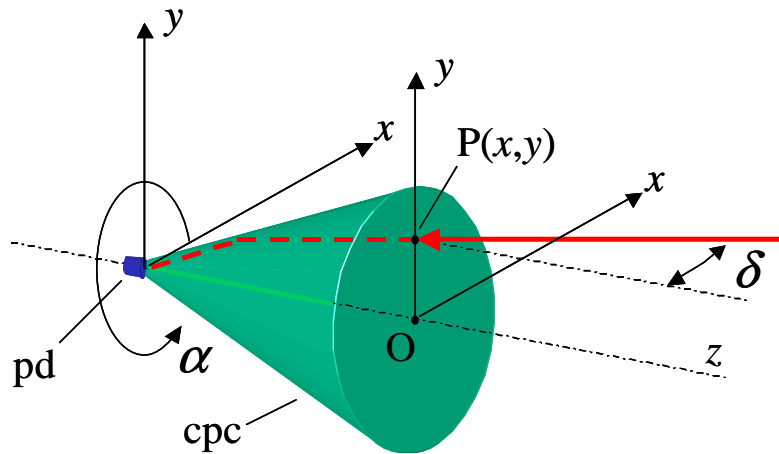
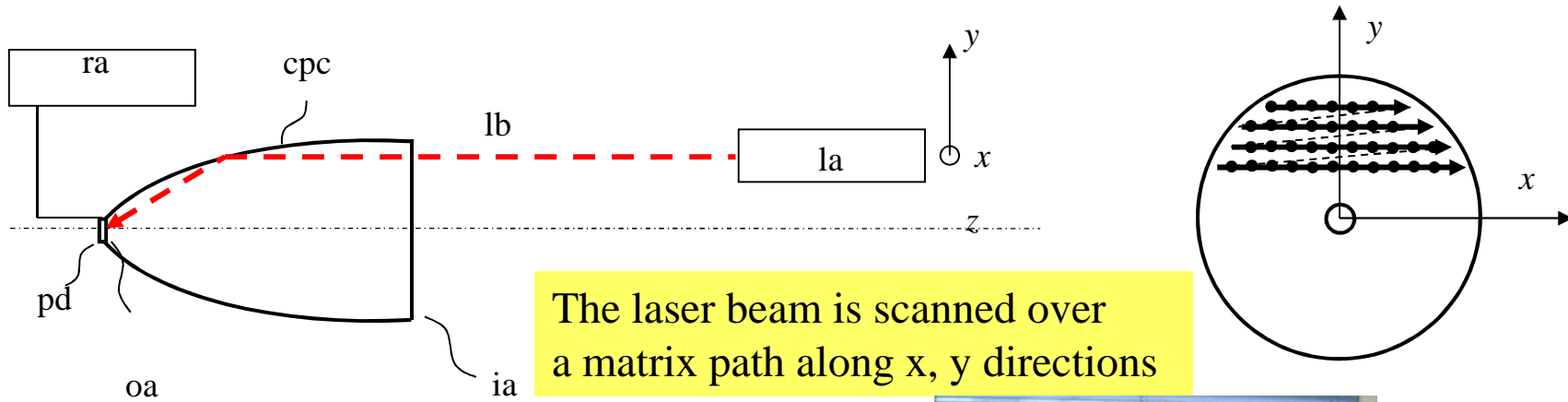


## THE “DIRECT LASER METHOD” (DLM)

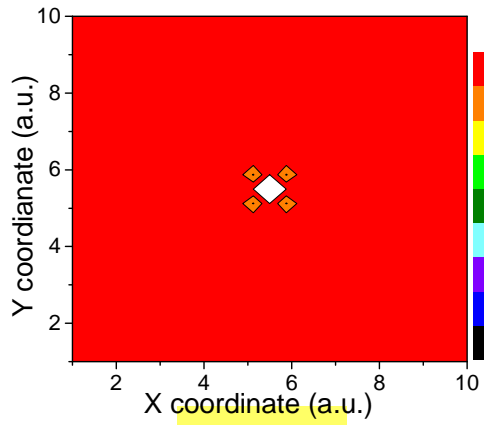


*Local (directional) transmission efficiency*

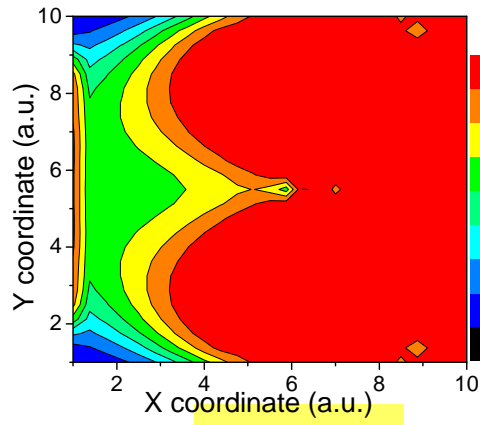
# The laser method (LM)



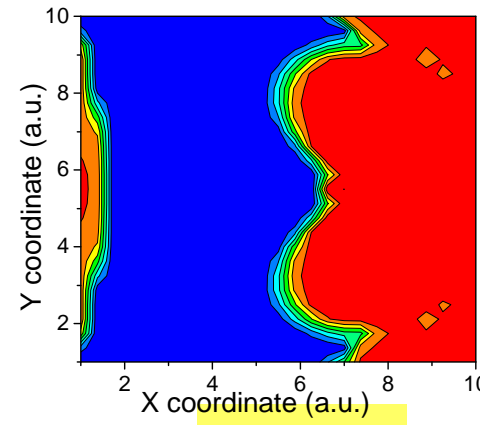
# Maps of optical efficiency ( $\alpha = 0^\circ$ )



$\delta = 0^\circ$

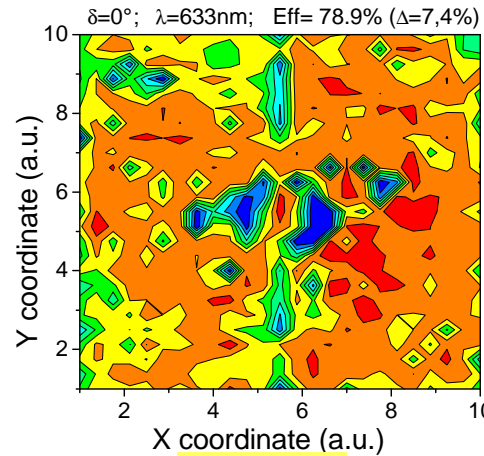


$\delta = 1.5^\circ$

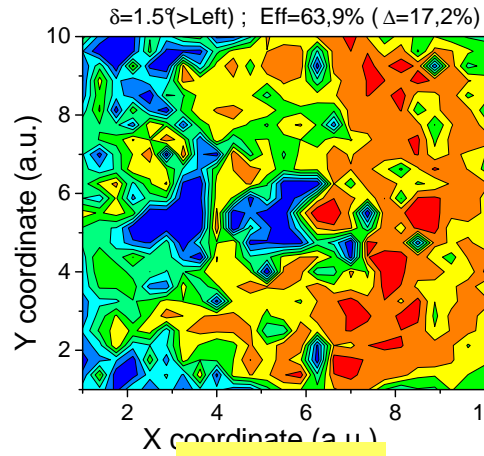


$\delta = 2.5^\circ$

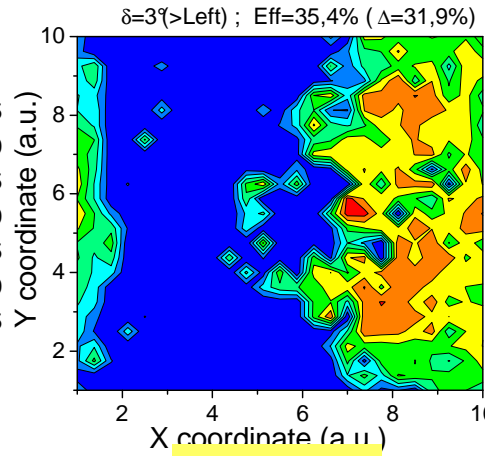
*Simulated*



$\delta = 0^\circ$



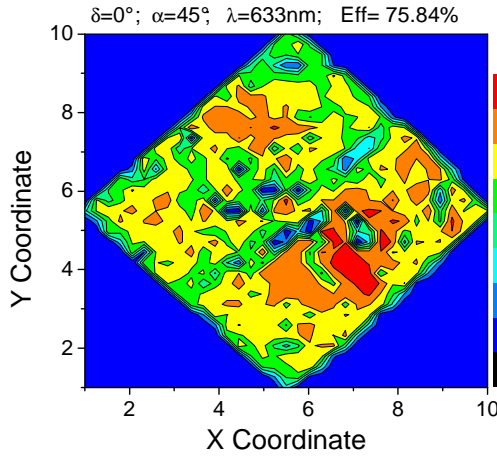
$\delta = 1.5^\circ$



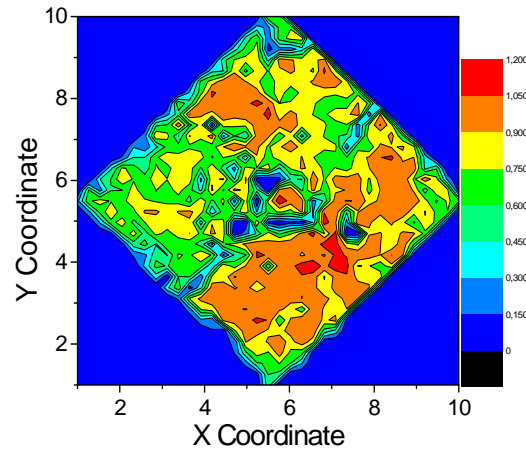
$\delta = 3.0^\circ$

*Experimental*

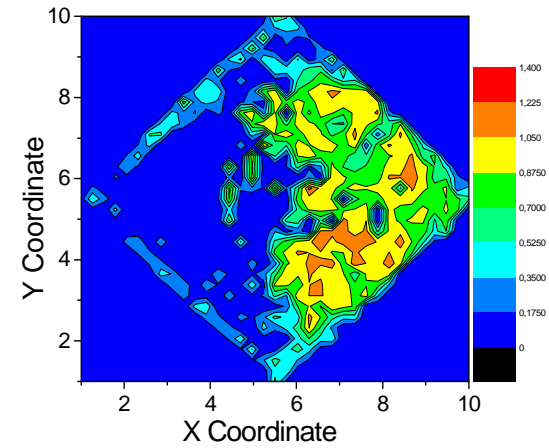
# Maps of optical efficiency ( $\alpha = 45^\circ$ )



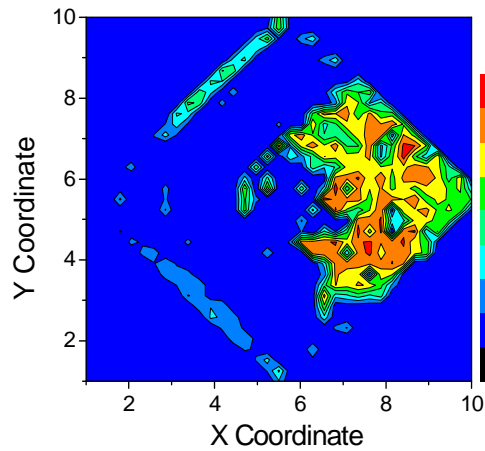
$\delta = 0^\circ$



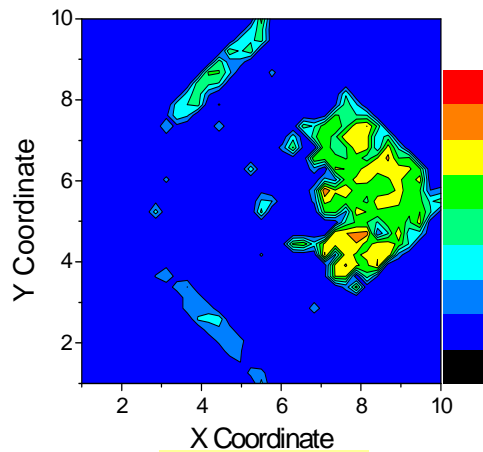
$\delta = 1.0^\circ$



$\delta = 2.0^\circ$



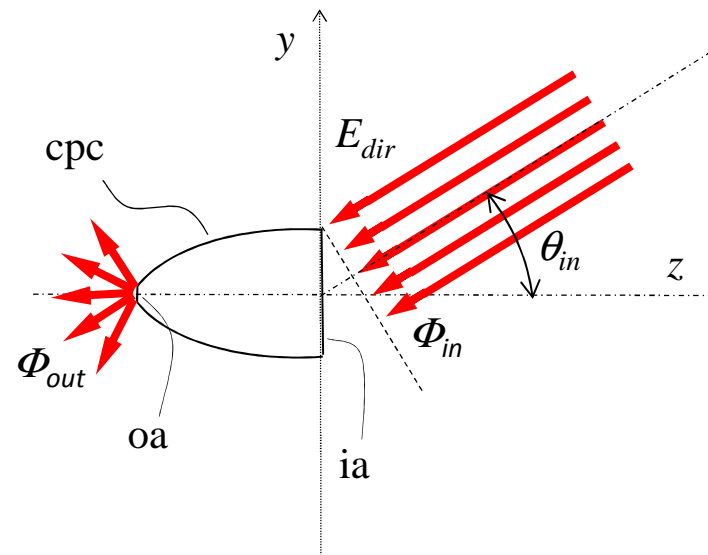
$\delta = 3.0^\circ$



$\delta = 4.0^\circ$

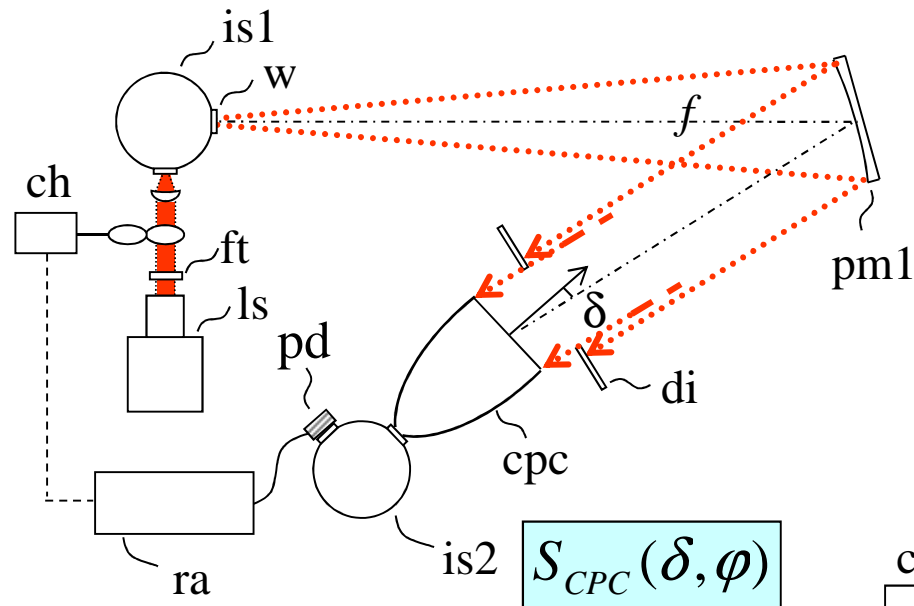
# THE “DIRECT COLLIMATED METHOD” (DCM)

(The typical operation of a solar concentrator!)



**Overall (directional) transmission efficiency**

# The experimental apparatus



Measurement of flux at output

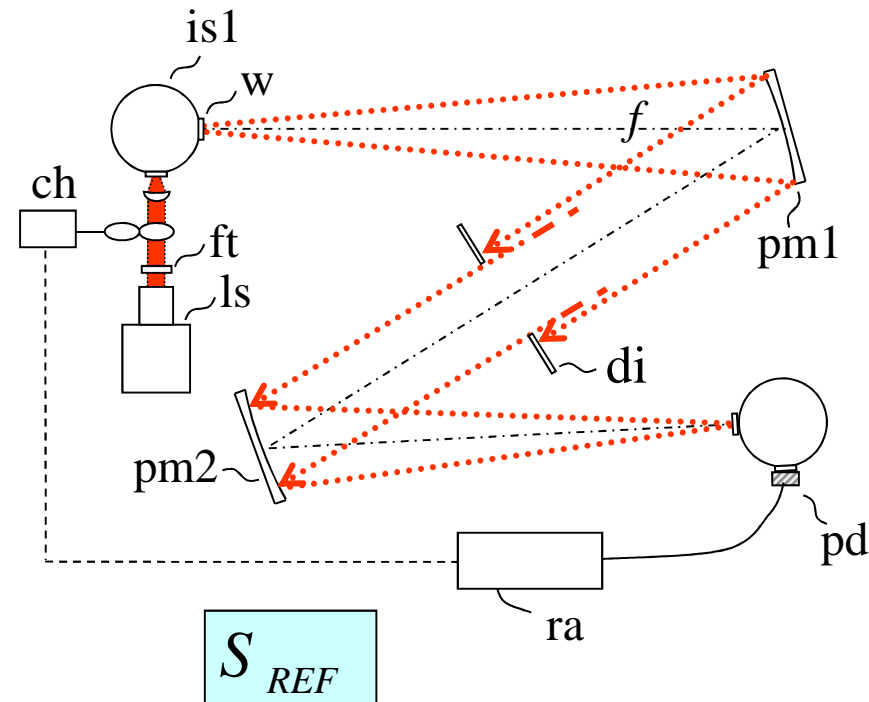
$$\eta(\delta, \varphi) = S_{CPC}(\delta, \varphi) \cdot \frac{R_{pm2}}{S_{REF} \cdot \cos \delta}$$

(Non-rotational symmetry)

$\left\{ \begin{array}{l} \delta = \text{polar angle} \\ \varphi = \text{azimuthal angle} \end{array} \right.$

$$\eta(\delta) = S_{CPC}(\delta) \cdot \frac{R_{pm2}}{S_{REF} \cdot \cos \delta}$$

(Rotational symmetry)



Measurement of flux at input

# Experimental apparatus (Ferrara Labs)

## Characterization of "Rondine" nonimaging concentrator



The source: two coupled integrating spheres

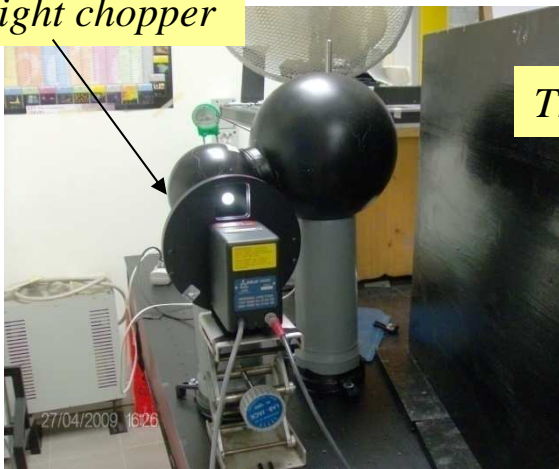
A lamp is placed inside the big sphere



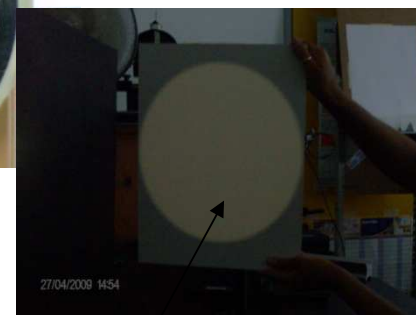
A fan is used to cool the spheres



The light chopper



The parabolic mirror

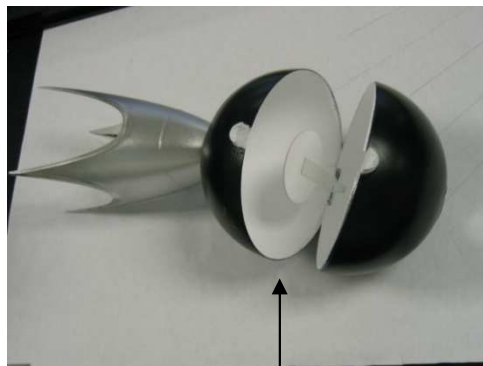


A uniform beam is produced



# Experimental apparatus (Ferrara Labs)

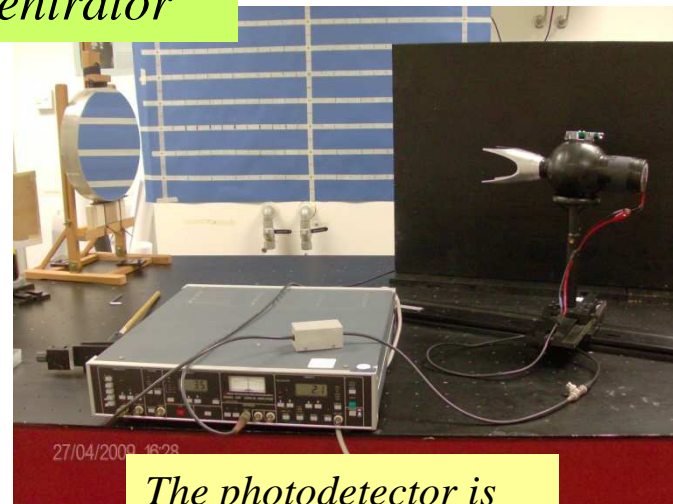
## Characterization of "Rondine" nonimaging concentrator



*The Rondine is coupled to an integrating sphere*



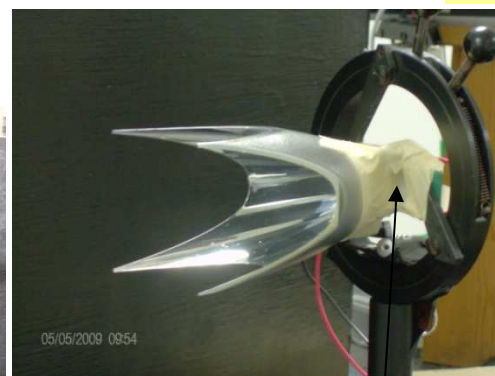
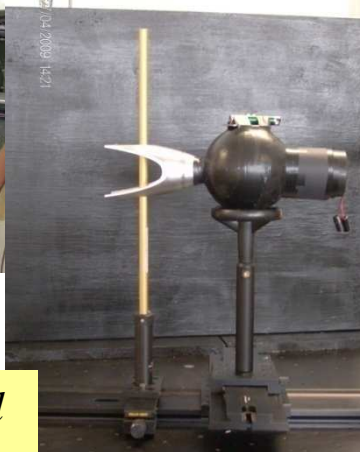
*A photodetector is placed inside the integrating sphere*



*The photodetector is connected to a lock-in*



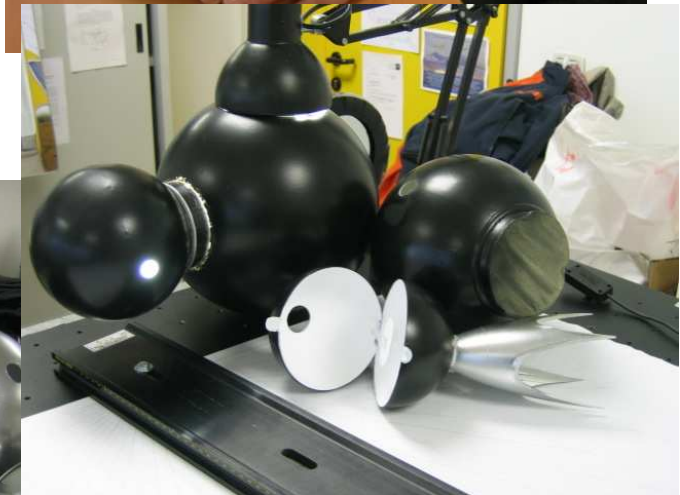
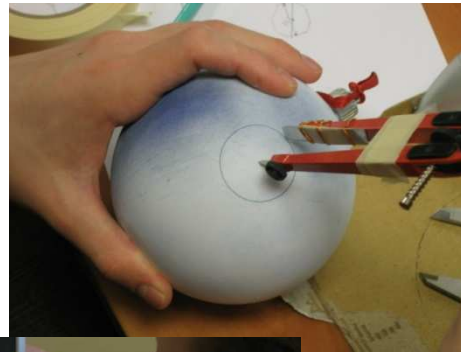
*The Rondine is aligned respect to the beam*



*Here the Rondine concentrator is directly coupled to a solar cell*

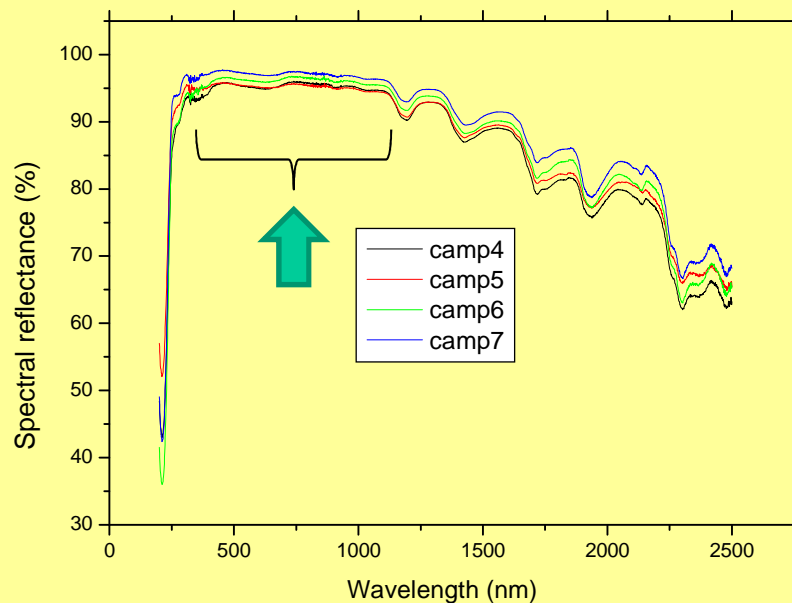


## Realization of the integrating spheres (Ferrara Labs)



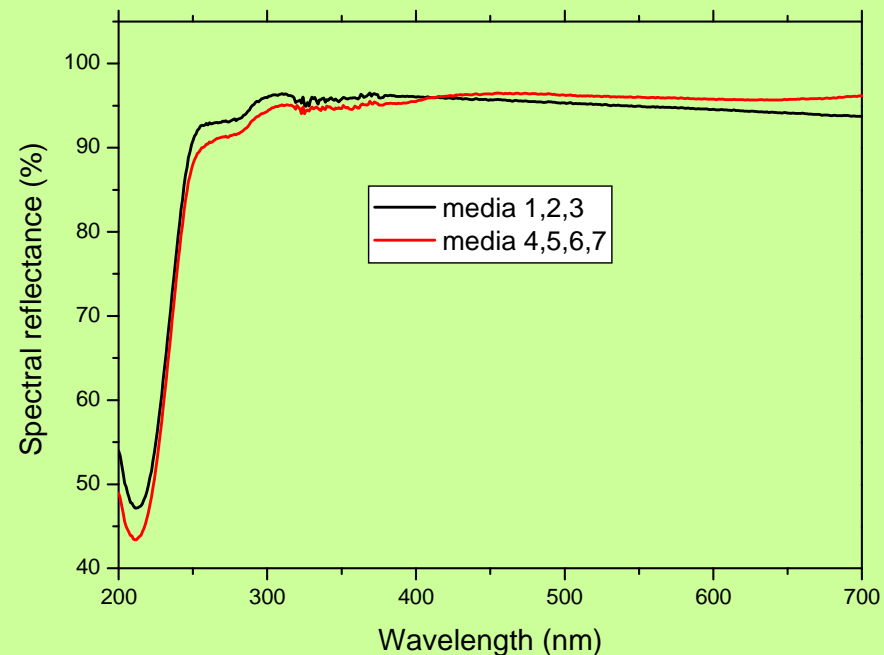
*All the integrating spheres were realized from plastic globes by using different paintings. The internal wall was painted by Barium Sulfate.*

# Optical properties of the integrating spheres



*Very good response at Vis-NIR!*

*Home-made BaSO<sub>4</sub>  
coatings*

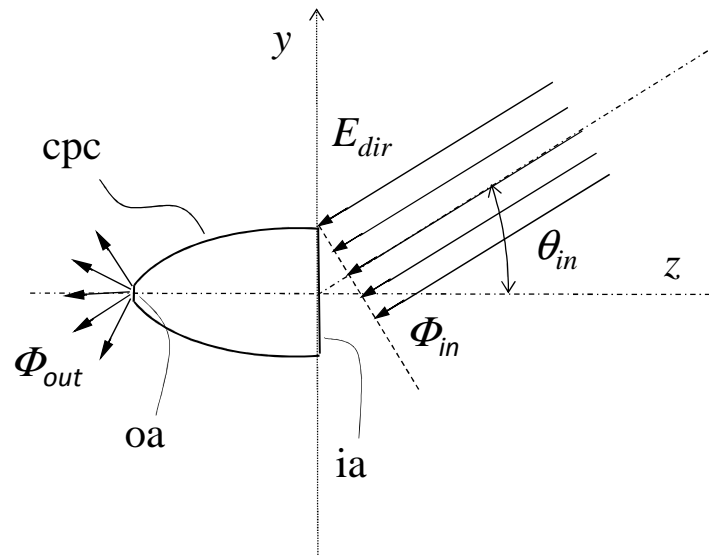


*Excellent response at UV!*

## TRANSMISSION EFFICIENCY OF A SOLAR CONCENTRATOR (Direct Collimated Method)

The fundamental quantity which summarizes the optical collection properties of a solar concentrator (SC) is the (angle-resolved) transmission efficiency:

$$\eta_{dir}(\theta_{in}, \varphi_{in}) = \frac{\Phi_{out}(\theta_{in}, \varphi_{in})}{\Phi_{in}(\theta_{in}, \varphi_{in})} = \frac{\Phi_{out}(\theta_{in}, \varphi_{in})}{E_{dir} \cdot A_{in}(\theta_{in}, \varphi_{in})}$$



Schematic principle of Direct Collimated Method (DCM).

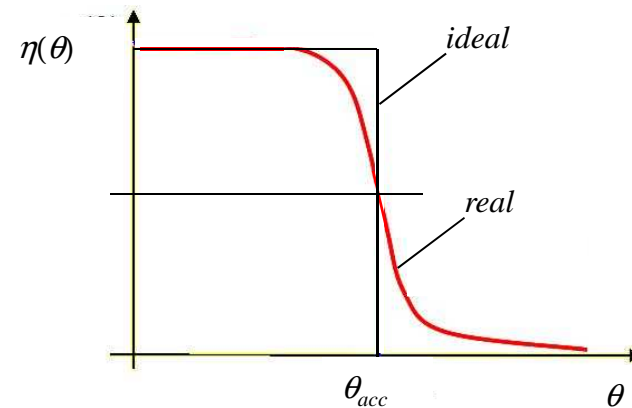
The SC is irradiated by a collimated beam oriented at  $\theta_{in}$  zenithal angle,  $\varphi_{in}$  azimuthal angle.

$E_{dir}$ : irradiance at the wavefront.

$\Phi_{in}$ : input flux.

$\Phi_{out}$ : output flux.

$A_{in}(\theta_{in}, \varphi_{in})$ : projected input area.



Example of transmission efficiency curve of a 3D-CPC concentrator. 20

## ANGLE-RESOLVED PROPERTIES OF A SOLAR CONCENTRATOR

In general we have:

Transmission efficiency:  $\eta_{dir}(\theta_{in}, \varphi_{in})$  = fraction of transmitted flux:

$$\eta_{dir}(\theta_{in}, \varphi_{in}) = \frac{\Phi_{out}(\theta_{in}, \varphi_{in})}{\Phi_{in}(\theta_{in}, \varphi_{in})}$$

Absorption efficiency:  $\alpha_{dir}(\theta_{in}, \varphi_{in})$  = fraction of absorbed flux:

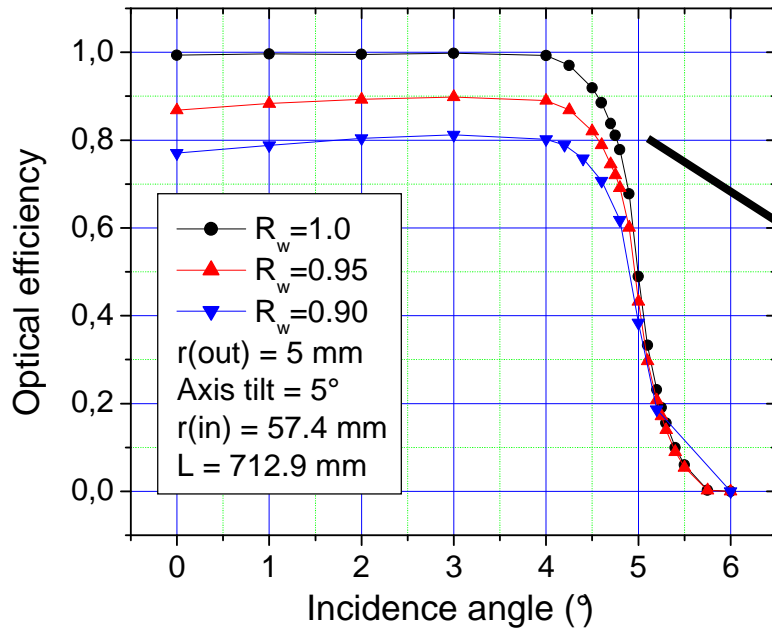
$$\alpha_{dir}(\theta_{in}, \varphi_{in}) = \frac{\Phi_{\alpha}(\theta_{in}, \varphi_{in})}{\Phi_{in}(\theta_{in}, \varphi_{in})}$$

Reflection efficiency:  $\rho_{dir}(\theta_{in}, \varphi_{in})$  = fraction of reflected flux:

$$\rho_{dir}(\theta_{in}, \varphi_{in}) = \frac{\Phi_{\rho}(\theta_{in}, \varphi_{in})}{\Phi_{in}(\theta_{in}, \varphi_{in})}$$

with:  $\eta_{dir}(\theta_{in}, \varphi_{in}) + \alpha_{dir}(\theta_{in}, \varphi_{in}) + \rho_{dir}(\theta_{in}, \varphi_{in}) = 1$

# Optical simulations of 3D-CPC with DCM

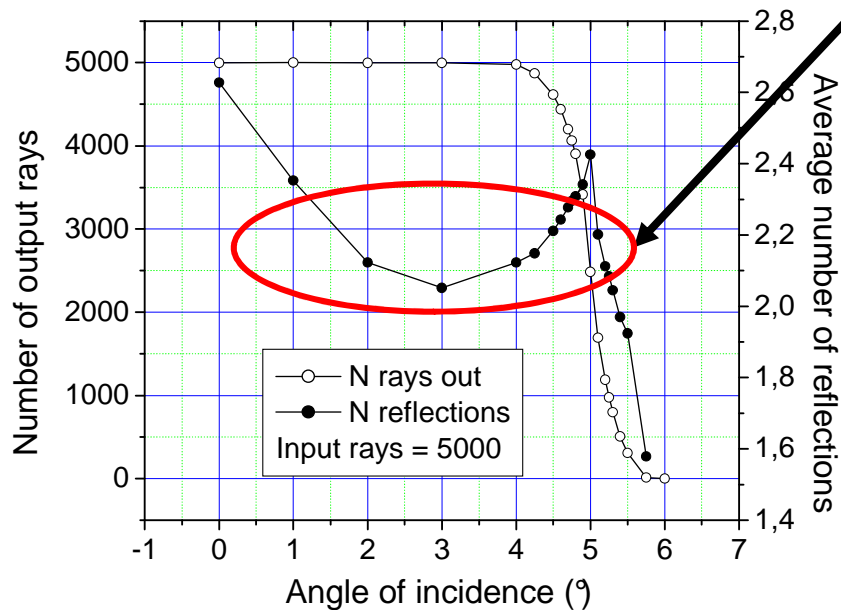


3D-CPC concentrator of 1-cm output diameter and  $5^\circ$ -axis tilt

Efficiency loss vs Reflectivity of the CPC walls:

$$-10\% R_w \rightarrow -20\% \eta(\theta)$$

Average number of reflections:  $\approx 2$ :



$$R_w = 1.0 \Rightarrow \eta(\delta) = \Phi_{out}(\delta) / \Phi_{in}$$

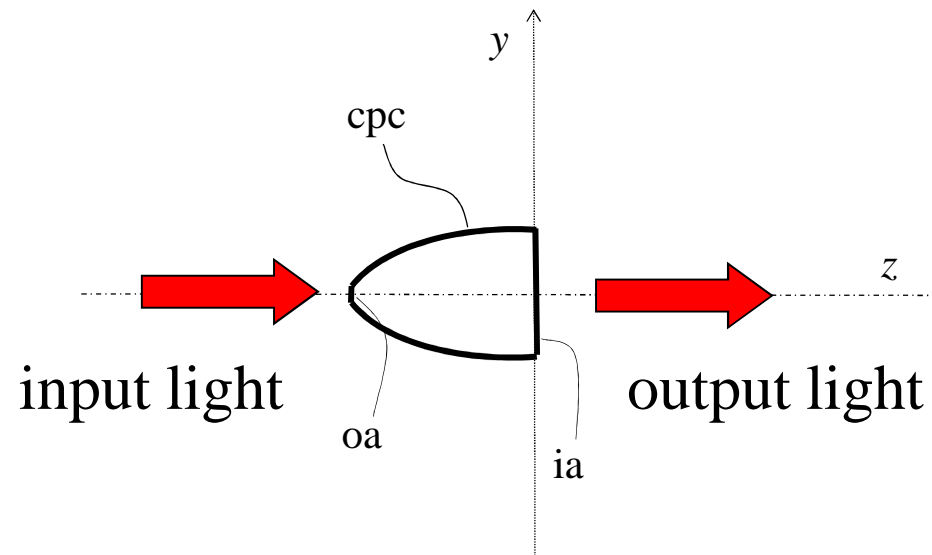
$$R_w' \Rightarrow \eta'(\delta) = \Phi'_{out}(\delta) / \Phi_{in} = \Phi_{out}(\delta) \cdot (R_w')^{\bar{N}(\delta)} / \Phi_{in}$$

$$R_w'' \Rightarrow \eta''(\delta) = \Phi''_{out}(\delta) / \Phi_{in} = \Phi_{out}(\delta) \cdot (R_w'')^{\bar{N}(\delta)} / \Phi_{in}$$

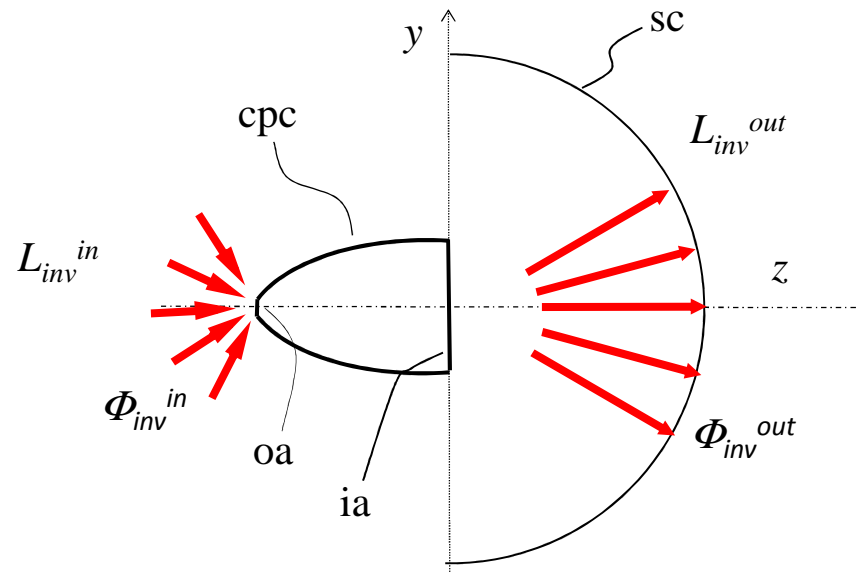
$$\bar{N}(\delta) = \ln \left[ \frac{\eta'(\delta)}{\eta(\delta)} \right] / \ln \left[ \frac{R_w'}{R_w''} \right]$$

Average number of reflections  
From a pair of efficiency curves

# THE “INVERSE” METHODS OF CHARACTERIZATION



THE “INVERSE METHOD” (IM)  
or  
“ILLUME” (Inverse Illumination Method)



*Overall (directional) transmission efficiency*

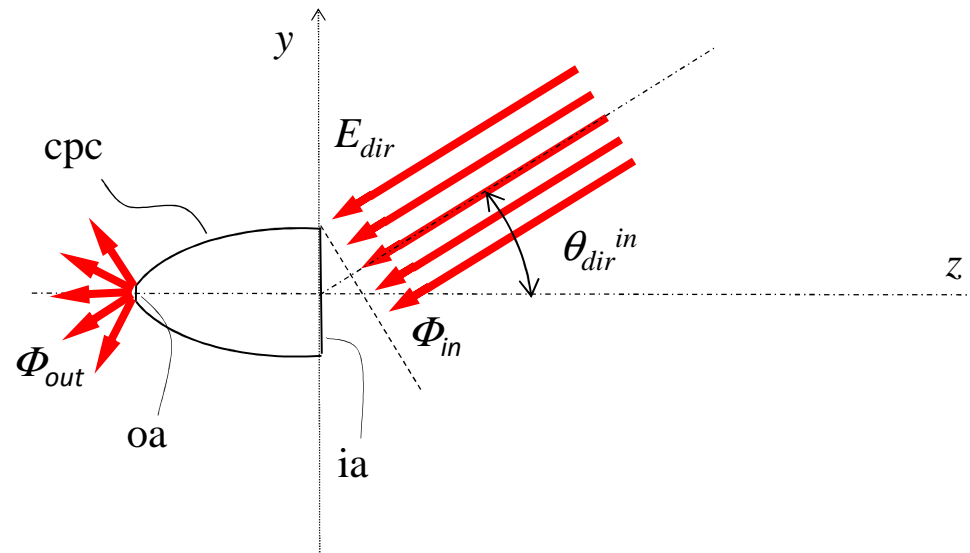
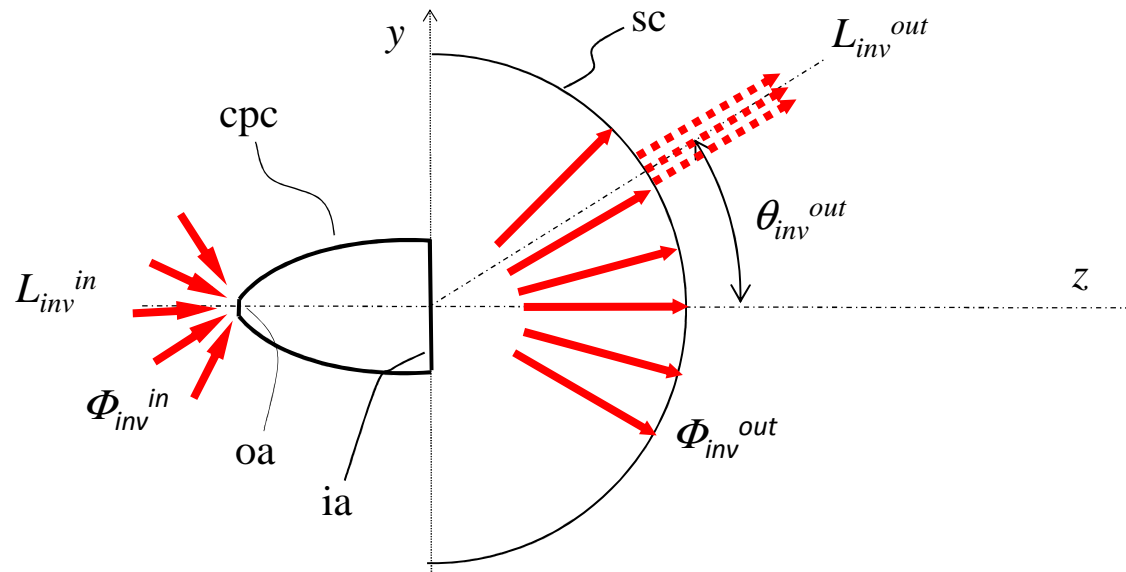


We can demonstrate that:

The “inverse” emission efficiency (the radiance)

=

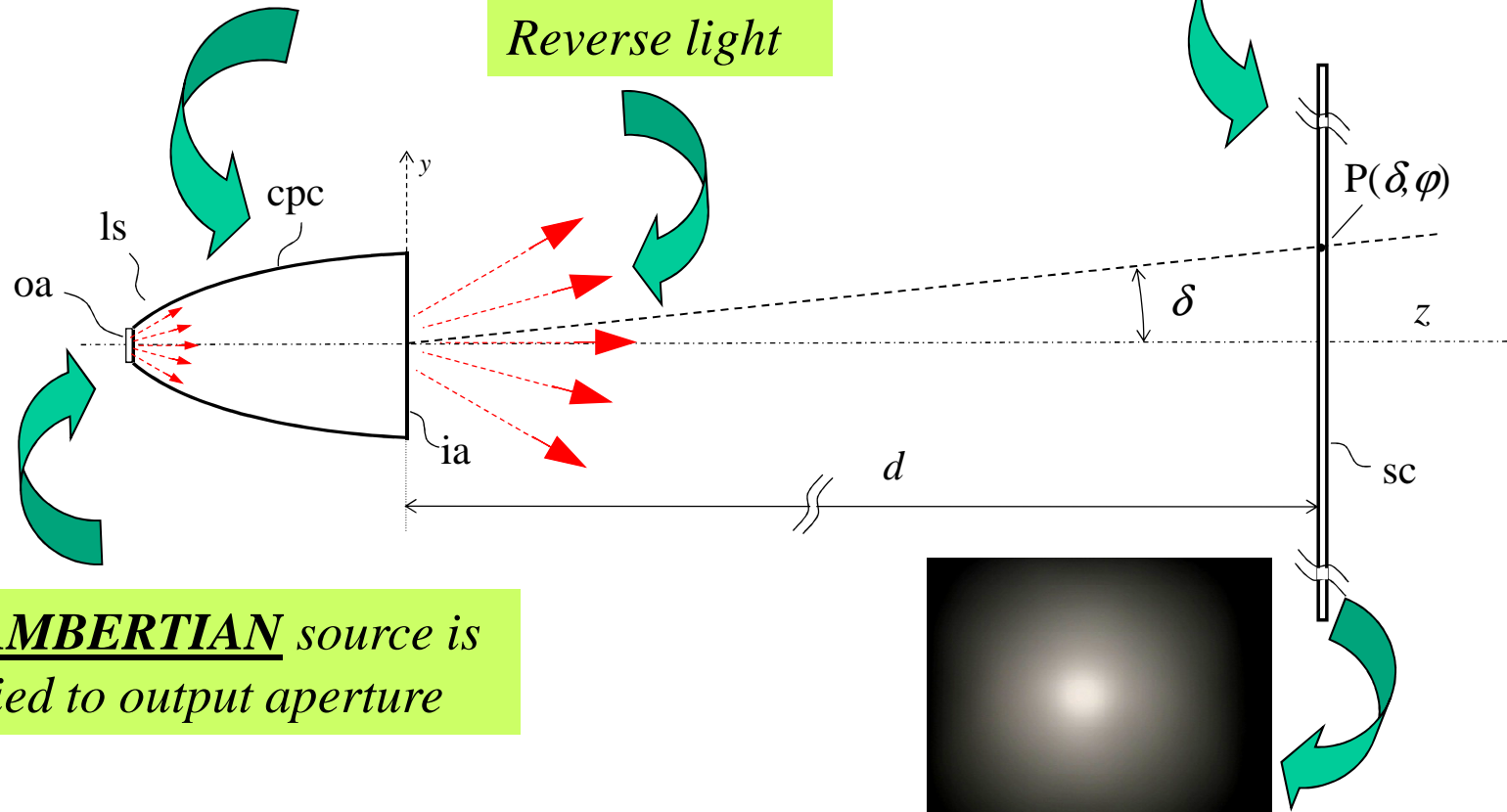
The “direct” collection (transmission) efficiency



# The basic principle of inverse method

*The concentrator becomes a source of light!*

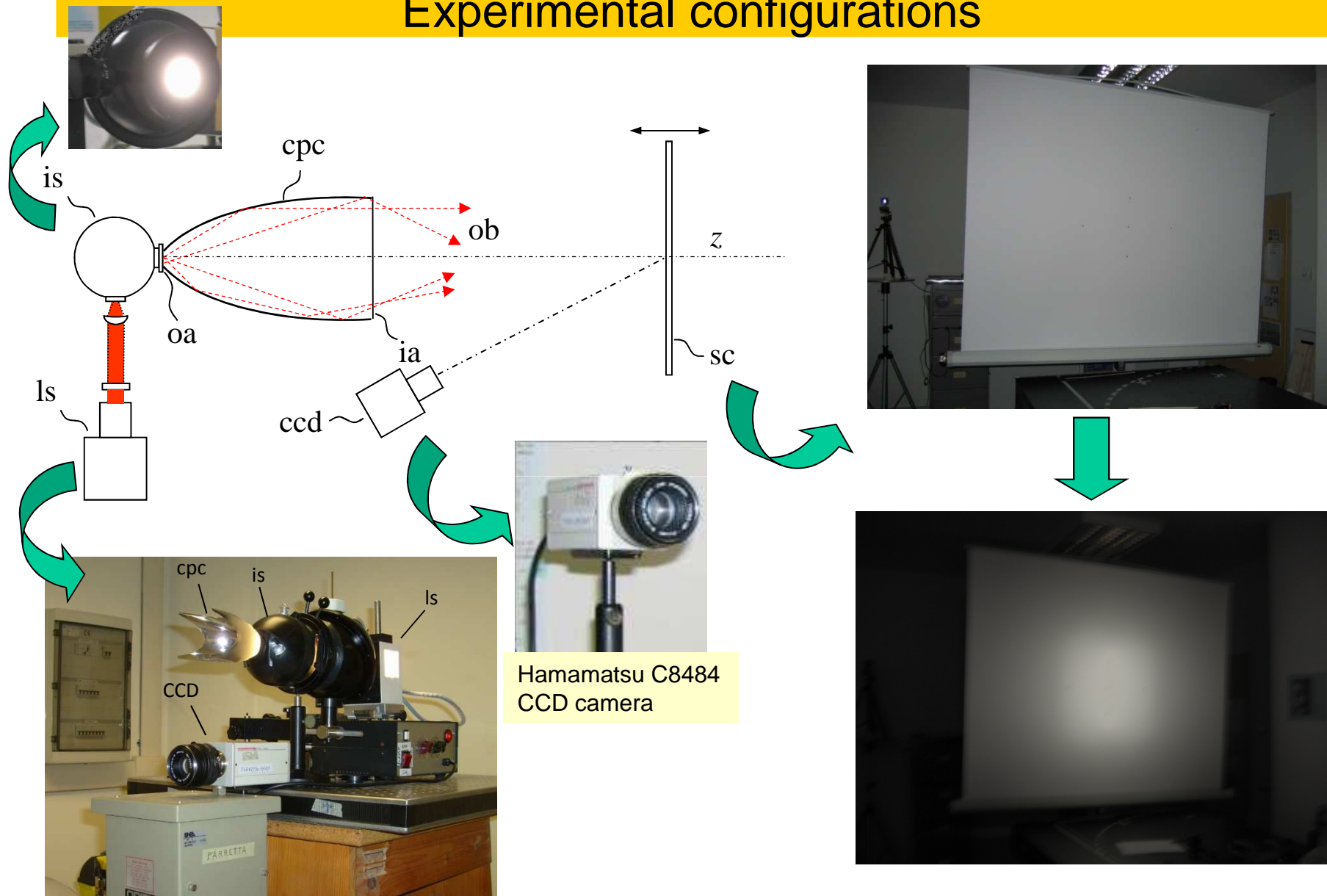
*A far Lambertian screen intercepts the reverse light*



*A **LAMBERTIAN** source is applied to output aperture*

*The image on the screen contains the overall information about the optical efficiency of concentrator*

# Experimental configurations



*Back illumination by an integrating sphere*

# Simplified theory of ILLUME (Ideal concentrator)

$\Phi_{in}(\delta)$ : flux at input

$\Phi_{out}(\delta, \varphi)$ : flux at output

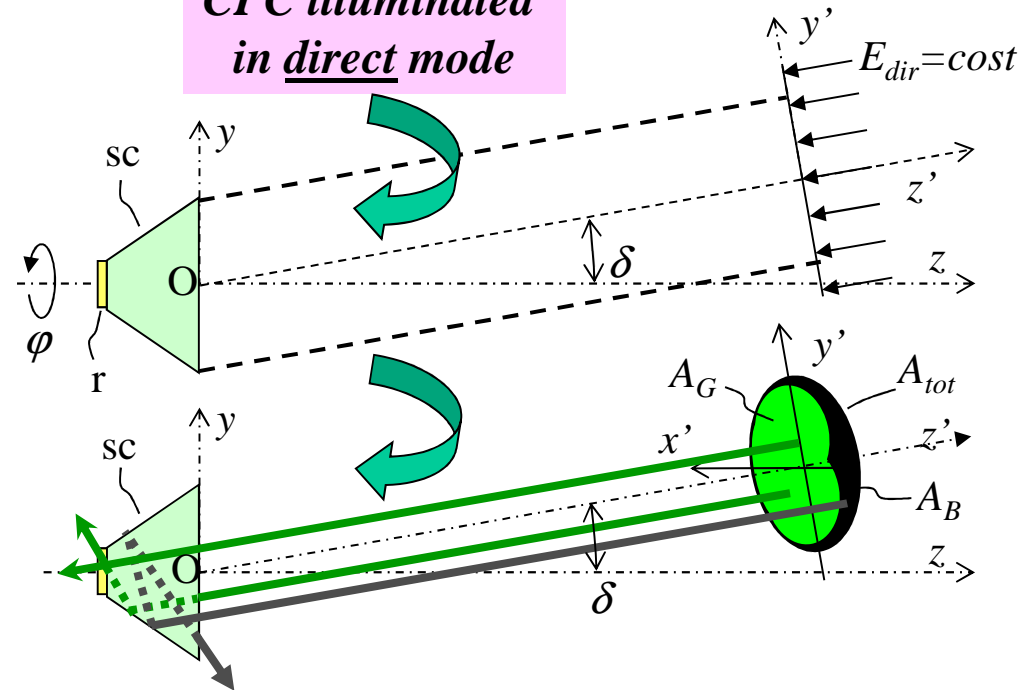
$$\eta(\delta, \varphi) = \Phi_{out}(\delta, \varphi) / \Phi_{in}(\delta)$$

**Forward rays at input are collected or rejected:**  
 Collected flux  $\propto$   
 to optical efficiency

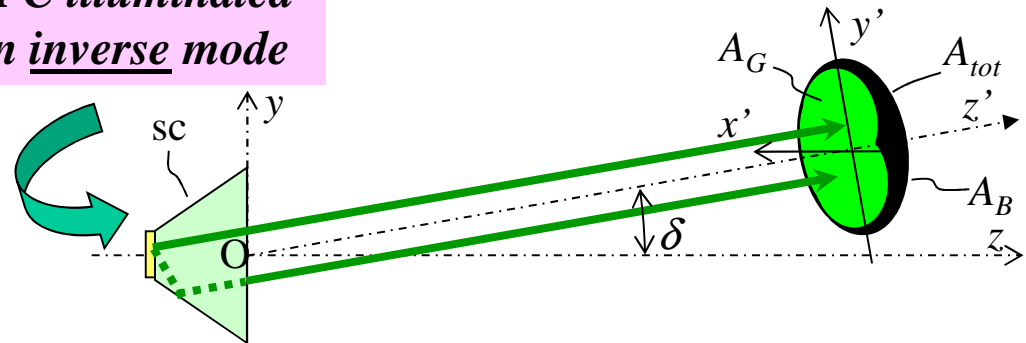
$$\eta(\delta, \varphi) = A_G(\delta, \varphi) / A_{tot}(\delta)$$

**Reverse rays at output are always collected:**  
 Emitted flux  $\propto$   
 to reverse radiance

CPC illuminated  
 in direct mode

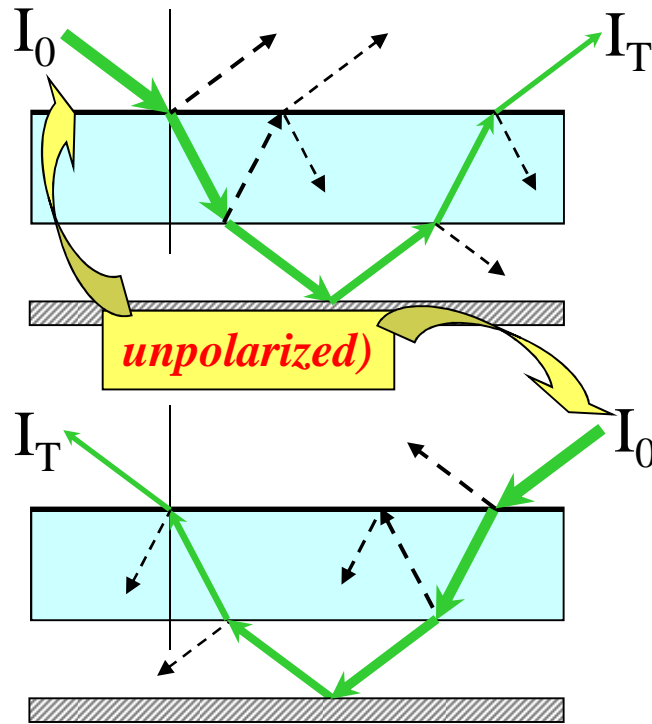


CPC illuminated  
 in inverse mode



**Reverse radiance  $\propto$  to optical efficiency!!!**

# Simplified theory of ILLUME (Real concentrator)



*Optical loss at interfaces  
inside the concentrator*

*For a real concentrator, we can apply the  
“reversibility principle” which establishes  
the same attenuation factor if the direction  
of light is reversed (and input light is unpolarized)*

**Reversibility Principle**

$I_T / I_0 = \text{attenuation factor} = \text{invariant}$

*For a single interface we can apply the Fresnel Equations:  
(R and T are invariant for exchange between indexes)*

*Attenuation of  
reflected ray*



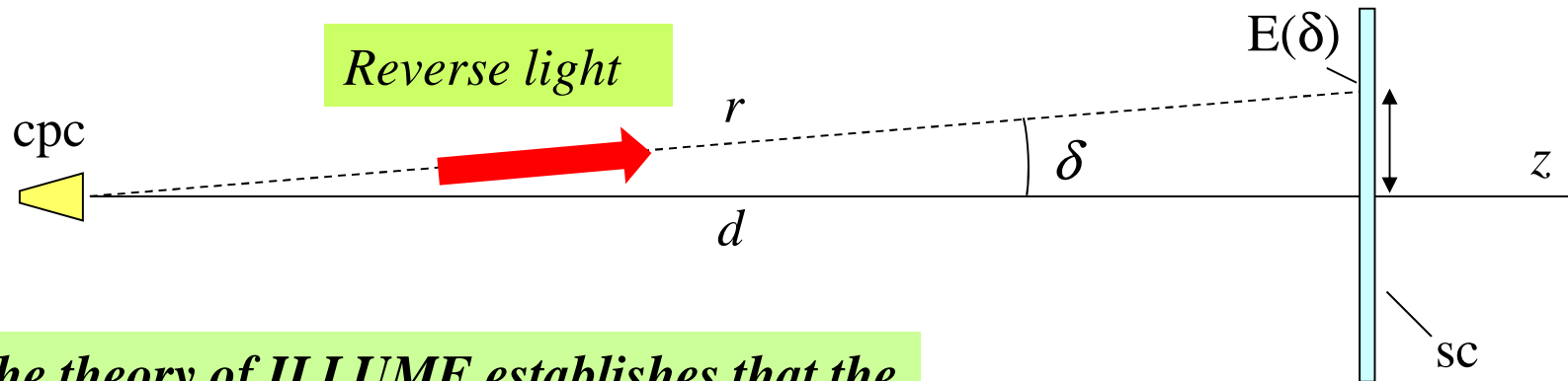
$$R = \frac{1}{2} \cdot (\rho_p^2 + \rho_s^2) = \frac{1}{2} \cdot \sin^2(\varphi - \varphi') \cdot \left[ \frac{\cos^2(\varphi + \varphi') + \cos^2(\varphi - \varphi')}{\sin^2(\varphi + \varphi') \cdot \cos^2(\varphi - \varphi')} \right]$$

*Attenuation of  
transmitted ray*



$$T = \frac{1}{2} \cdot \left( \frac{n'}{n} \right) \cdot \left( \frac{\cos \varphi'}{\cos \varphi} \right) \cdot (\tau_p^2 + \tau_s^2) = 2 \cdot \sin \varphi \cdot \sin \varphi' \cdot \cos \varphi \cdot \cos \varphi' \cdot \left[ \frac{1 + \cos^2(\varphi - \varphi')}{\sin^2(\varphi + \varphi') \cdot \cos^2(\varphi - \varphi')} \right]$$

# Simplified theory of ILLUME



*The theory of ILLUME establishes that the radiance of concentrator in the inverse mode is proportional to its transmission efficiency in direct mode!!*

$$L_{rel}^{inv}(\delta, \varphi) = \eta_{rel}(\delta, \varphi)$$

*How to calculate the radiance profile from the irradiance profile on the screen?  
Simply dividing by  $\cos^4(\delta)$*

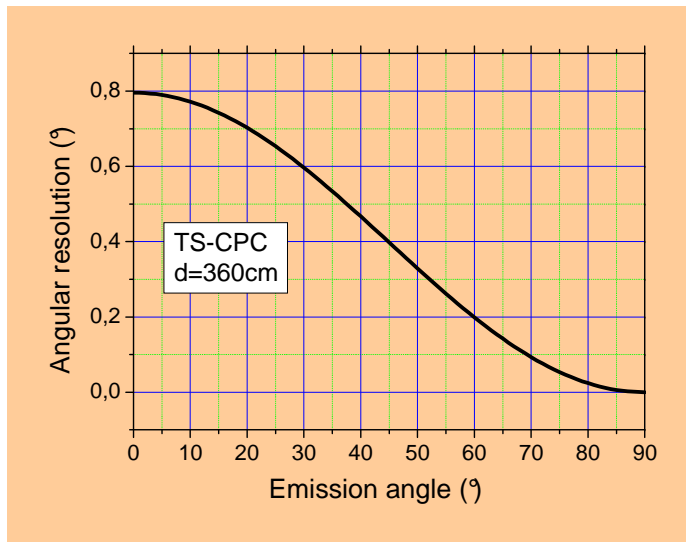
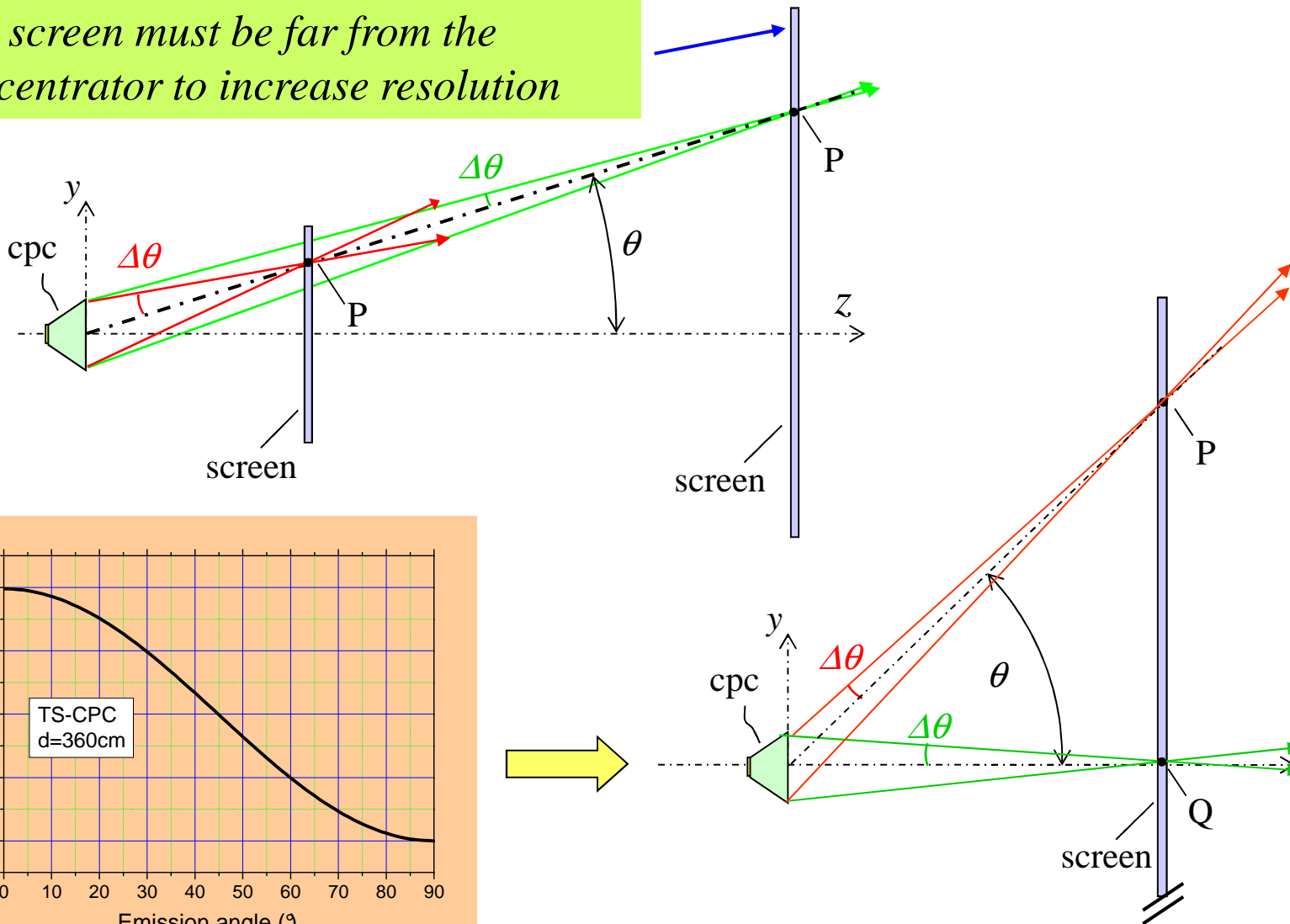
$$L_{inv}^{rel}(\delta, \varphi) = E_{inv}^{rel}(\delta, \varphi) \cdot \frac{1}{\cos^4 \delta}$$

*General formula:*

$$L_{rel}^{inv}(\delta, \varphi) = \frac{L^{inv}(\delta, \varphi)}{L^{inv}(0)} = \frac{\eta(\delta, \varphi)}{\eta(0)} = \eta_{rel}(\delta, \varphi)$$

# Simplified theory of ILLUME (Angular resolution)

*The screen must be far from the concentrator to increase resolution*

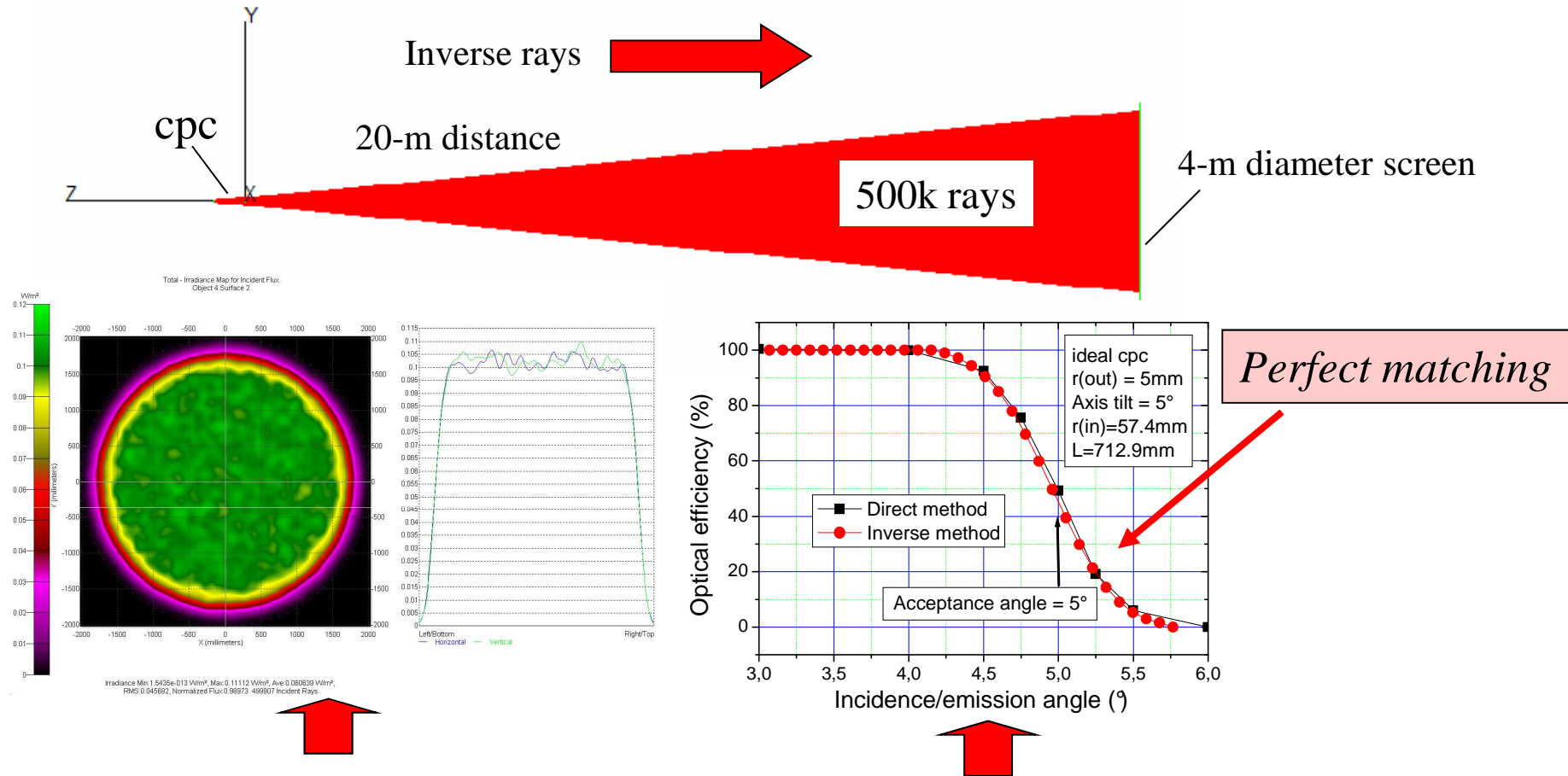


*The angular resolution improves for points on the screen with high  $\theta$  values*

APPLICATIONS  
OF DIRECT AND INVERSE  
METHODS



# Ideal 3D-CPC – Optical Simulations



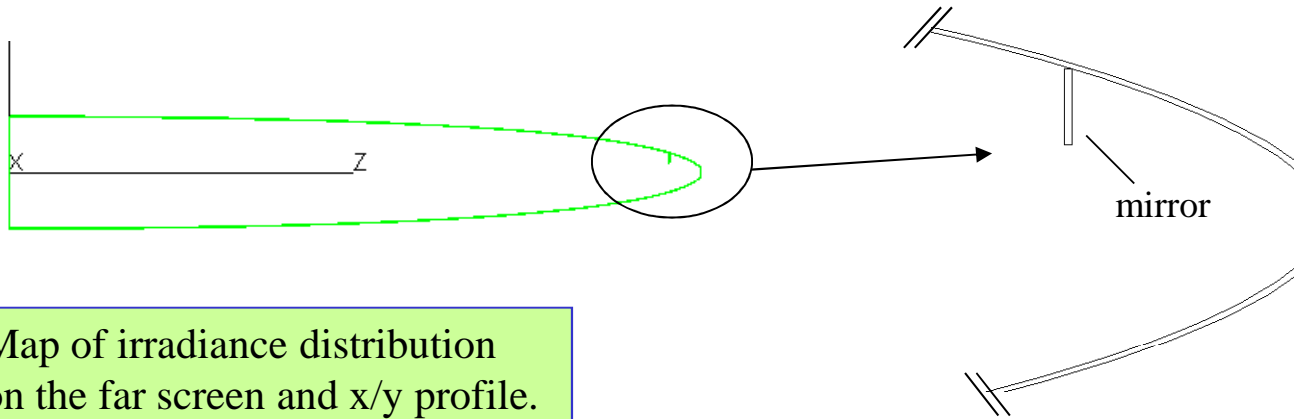
Map of irradiance distribution on the far screen and x/y profile.

Optical efficiency curves simulated for the direct and inverse method.

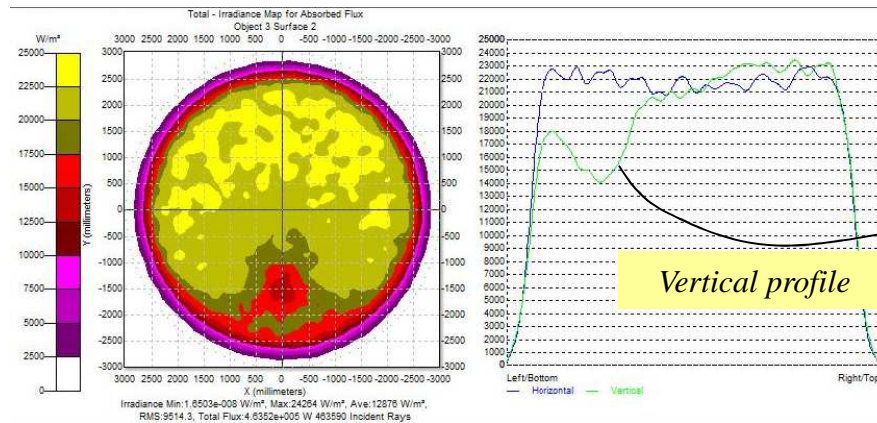
*The inverse method requires one simulation!!  
The direct method requires tens of simulations!!*

# Ideal 3D-CPC + mirror – Optical Simulations

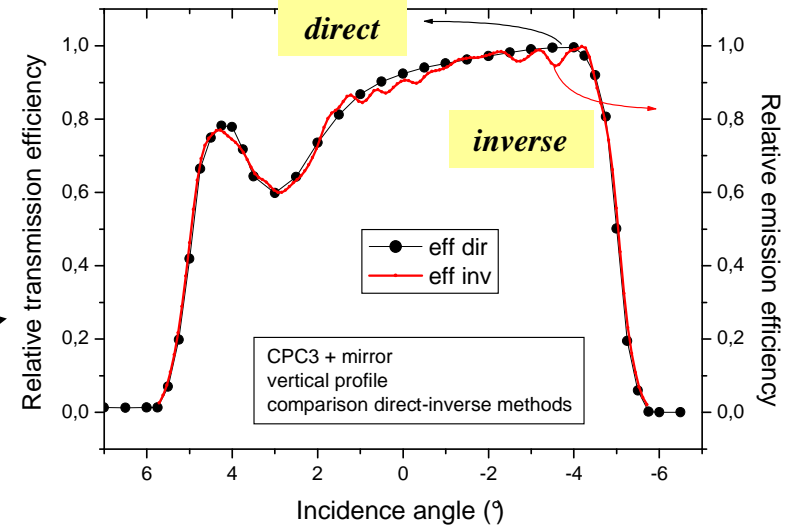
*The inverse method works well at any condition!  
To demonstrate it, we put an object (a mirror) inside the ideal concentrator and simulate again the direct and inverse methods*



Map of irradiance distribution on the far screen and x/y profile.

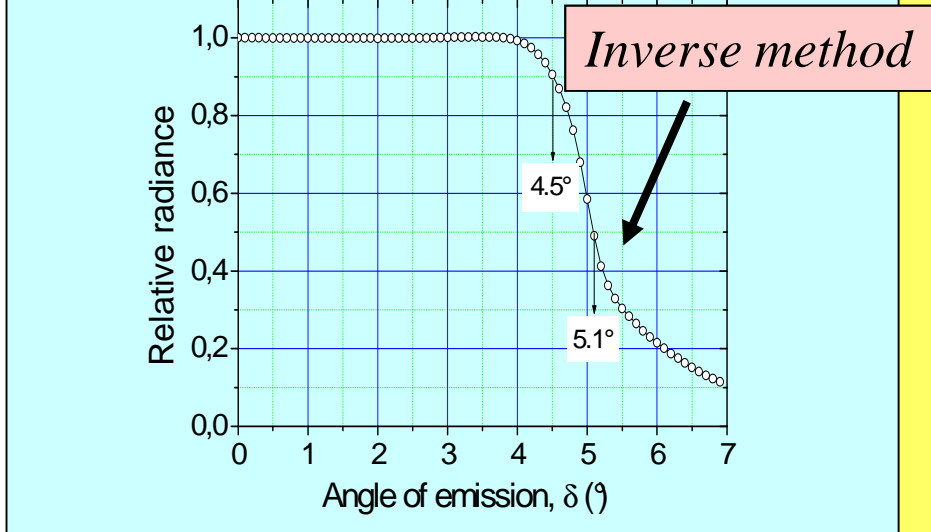
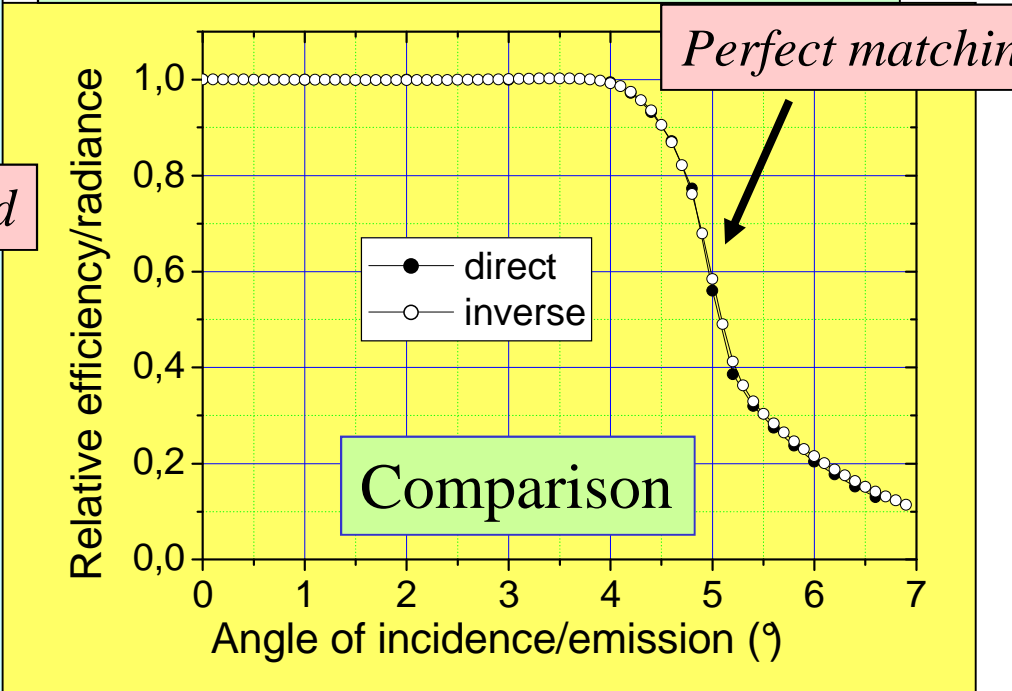
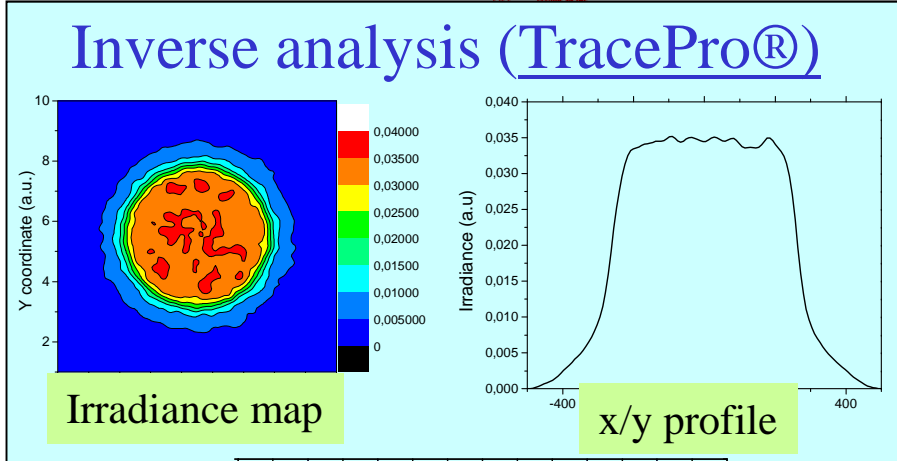
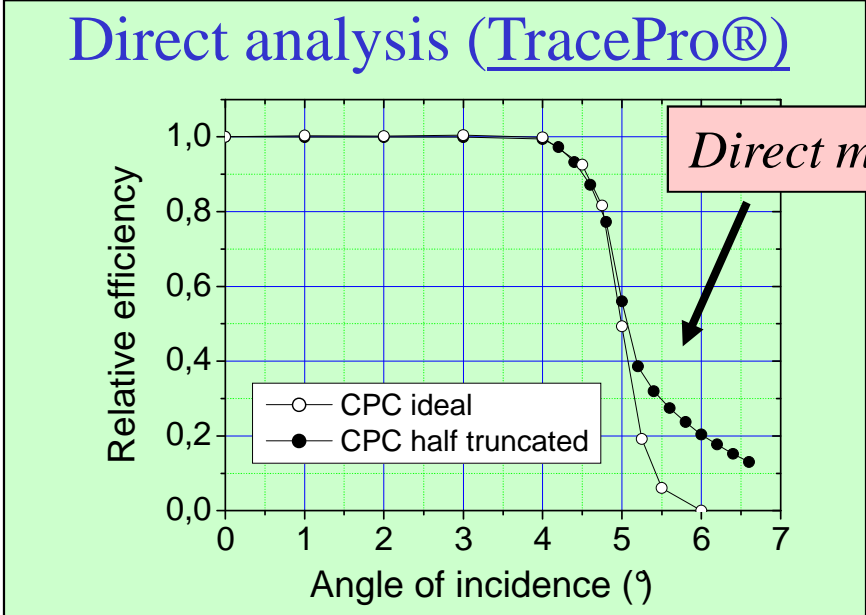
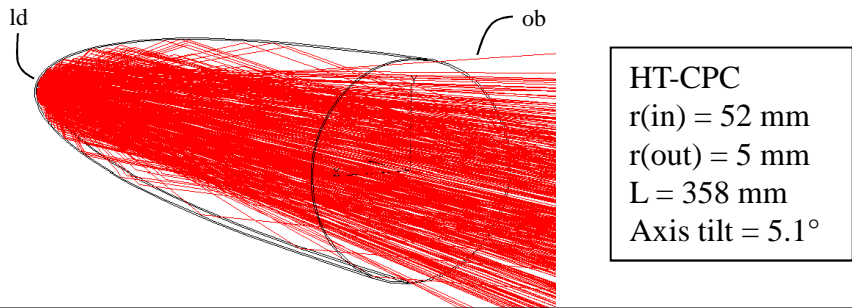


Map of inverse method



The vertical profiles are equal !!!

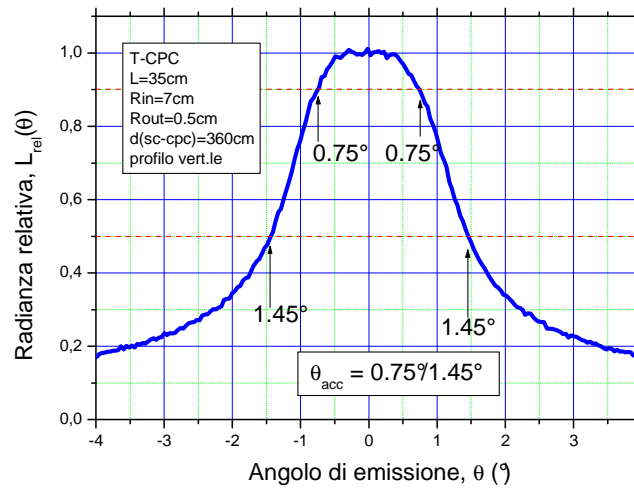
# Half-Truncated 3D-CPC (HT-CPC) – Optical Simulations



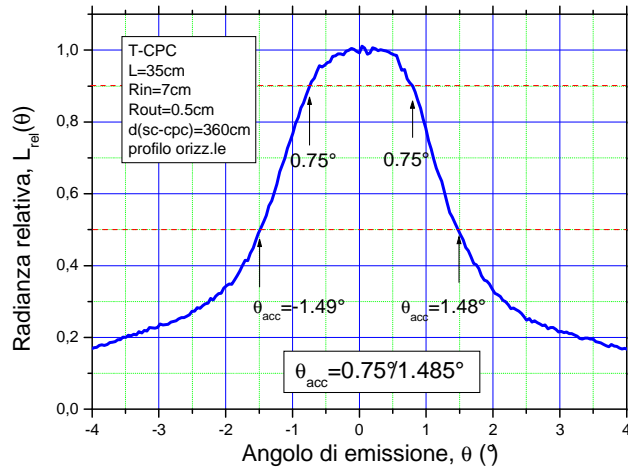
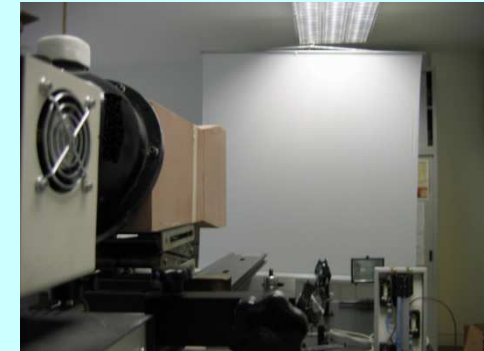
# Truncated 3D-CPC (T-CPC) – Experimental results



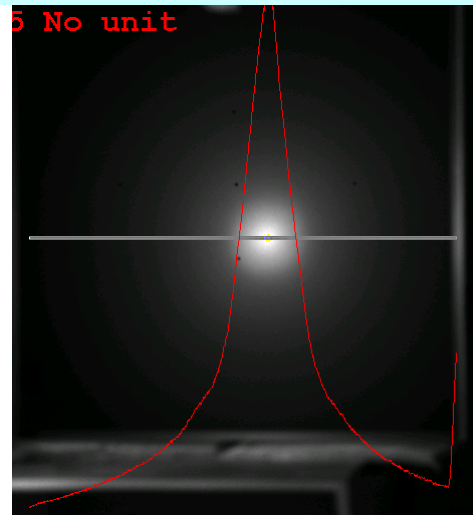
*Vertical profile*  
 $\theta_{acc} = 0.75^\circ / 1.45^\circ$



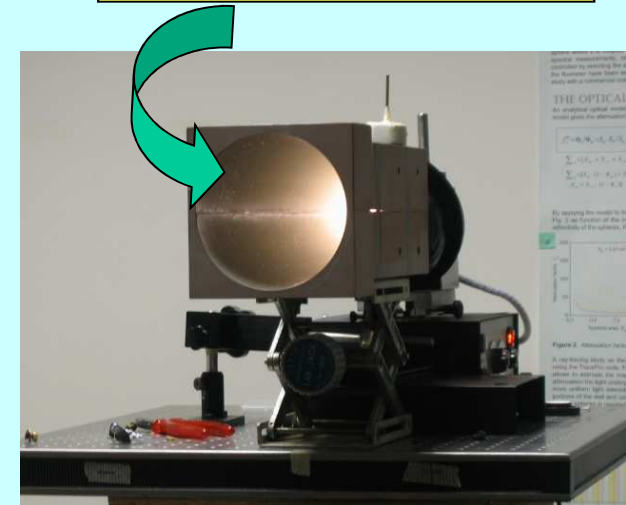
T-CPC  
 r(in) = 70 mm  
 r(out) = 5 mm  
 L = 358 mm



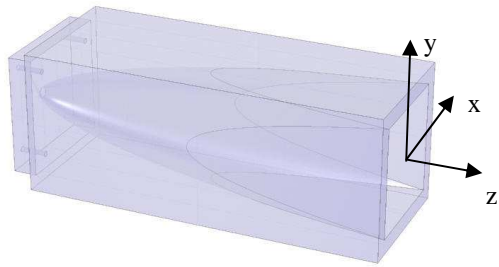
*Horizontal profile*  
 $\theta_{acc} = 0.75^\circ / 1.48^\circ$



No mirror in the inner wall !!

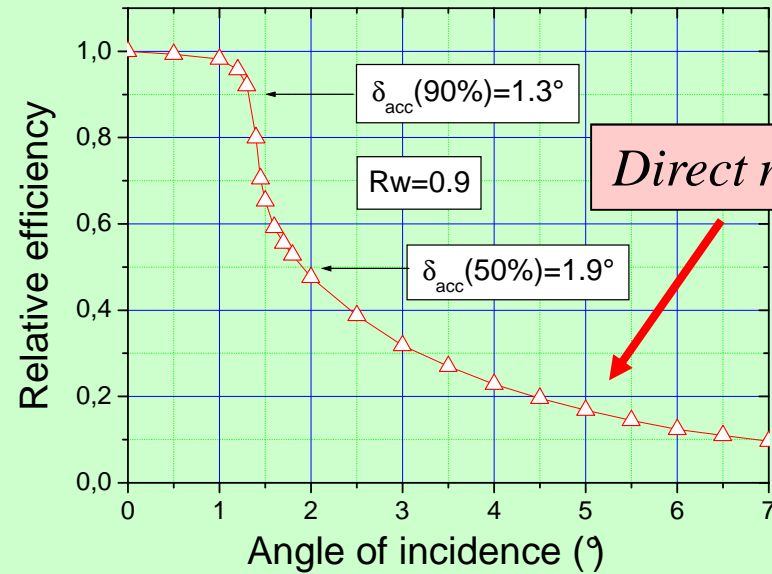


# Truncated and Squared CPC (TS-CPC) – Optical Simulations

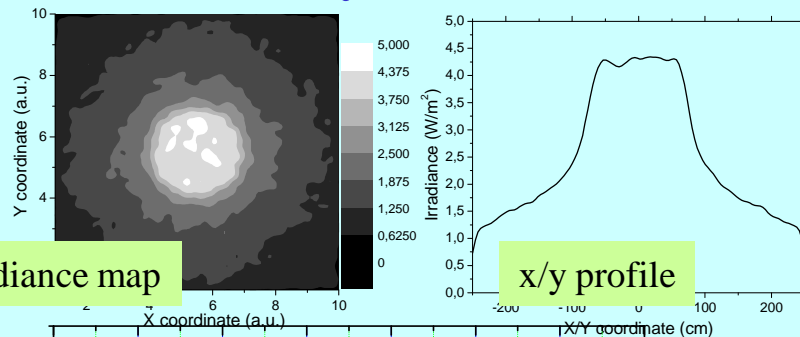


TS-CPC  
 $l(\text{in}) = 100 \text{ mm}$   
 $r(\text{out}) = 5 \text{ mm}$   
 $L = 350 \text{ mm}$

## Direct analysis (TracePro®)

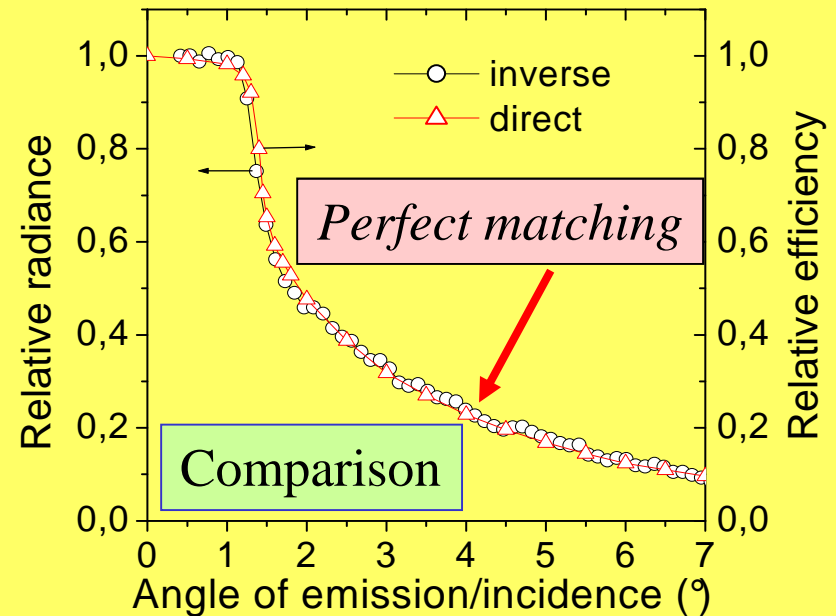
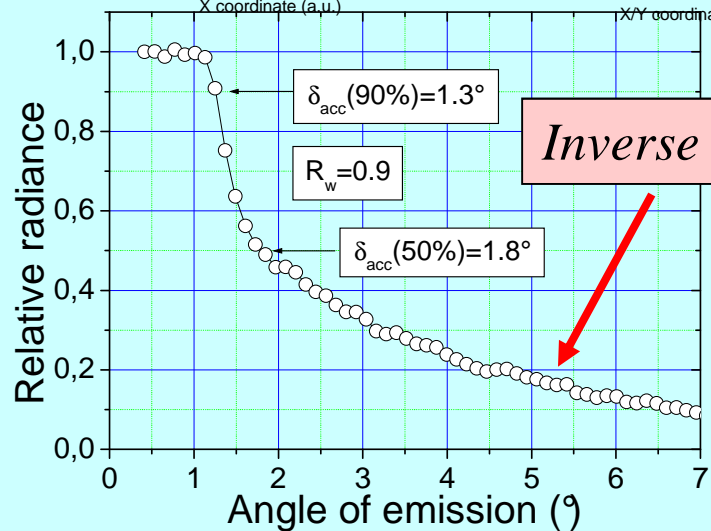


## Inverse analysis (TracePro®)



Irradiance map

*Inverse method*

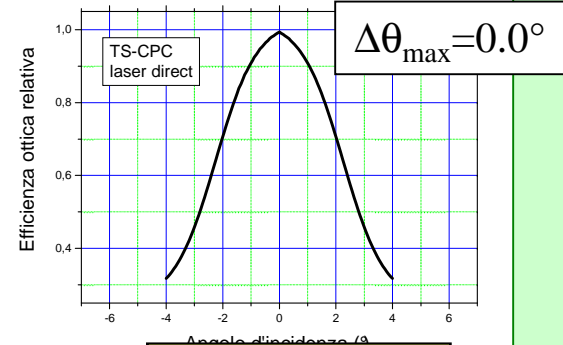


# Truncated and Squared CPC (TS-CPC) – Experiments

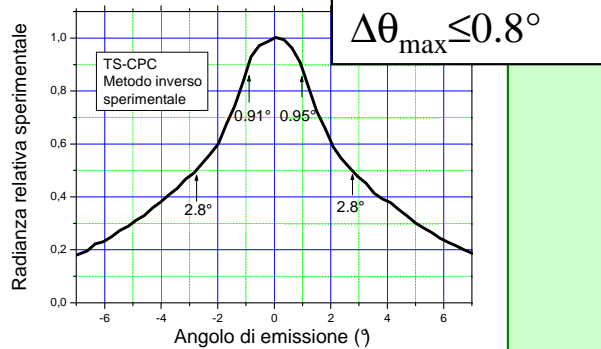


Back illumination by an integrating sphere

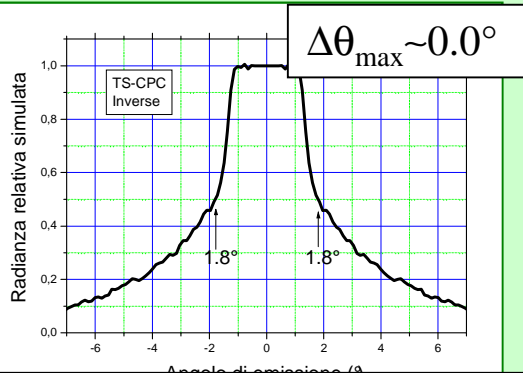
Light projected on the planar screen



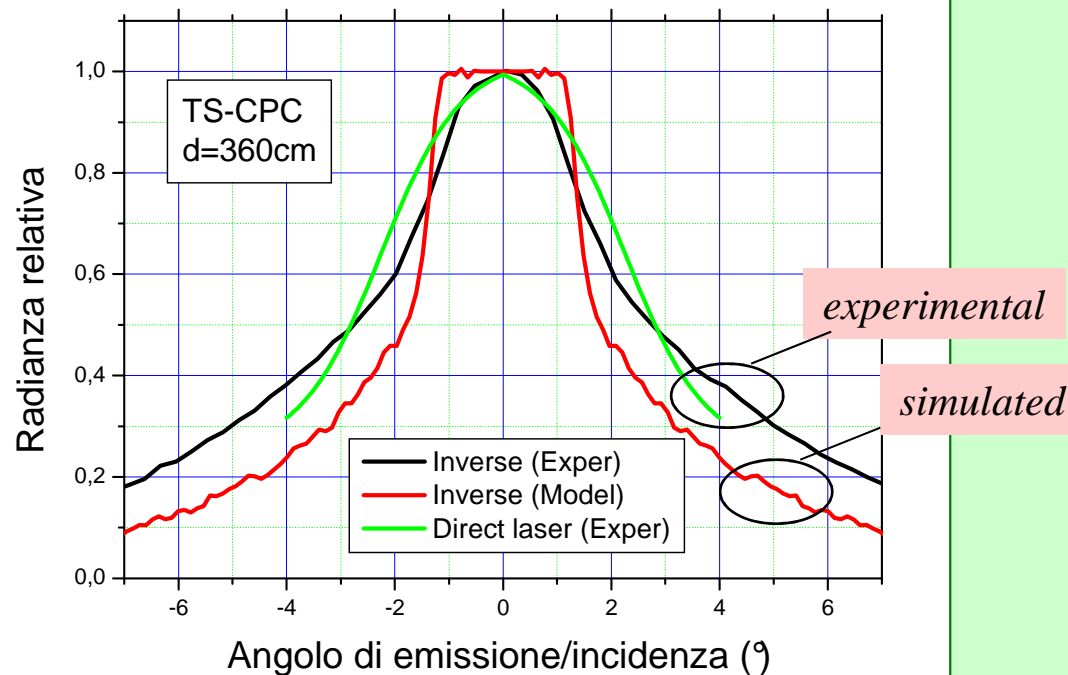
Laser method



Inverse experimental

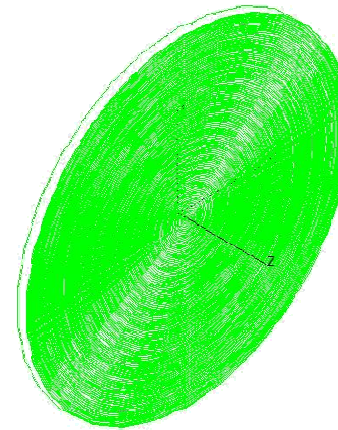
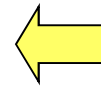
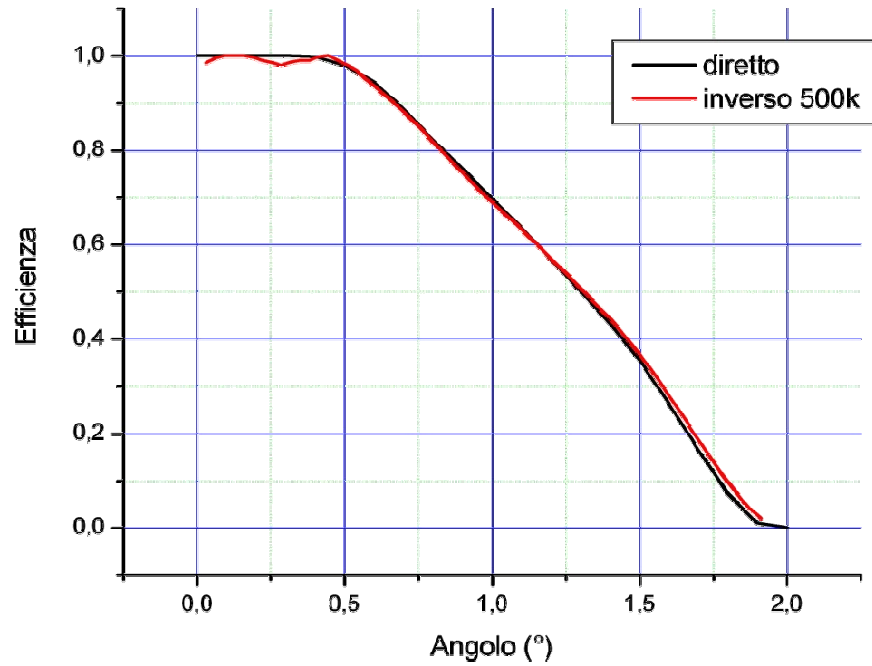


Direct and Inverse simulated



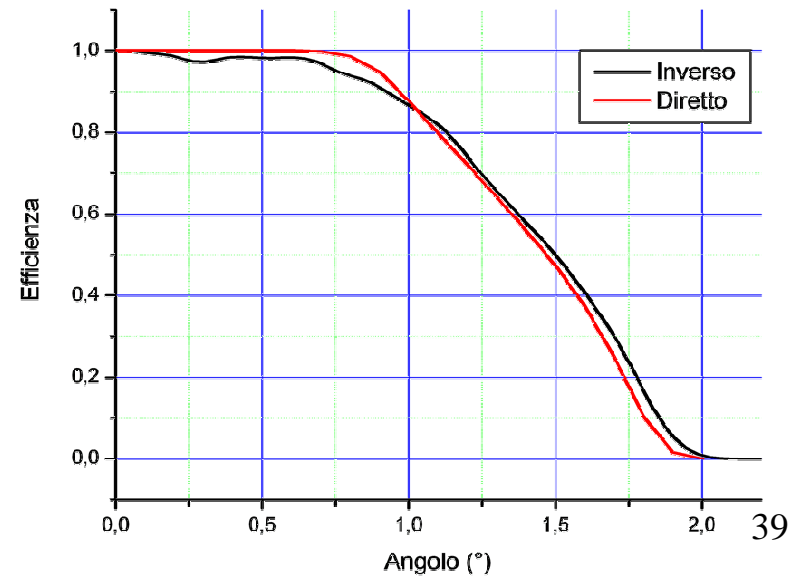
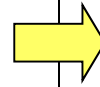
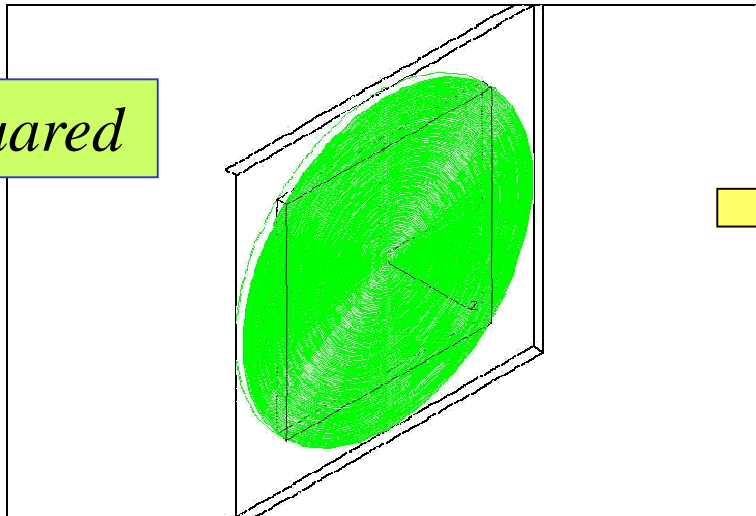
Comparison among the different methods

# Fresnel lens

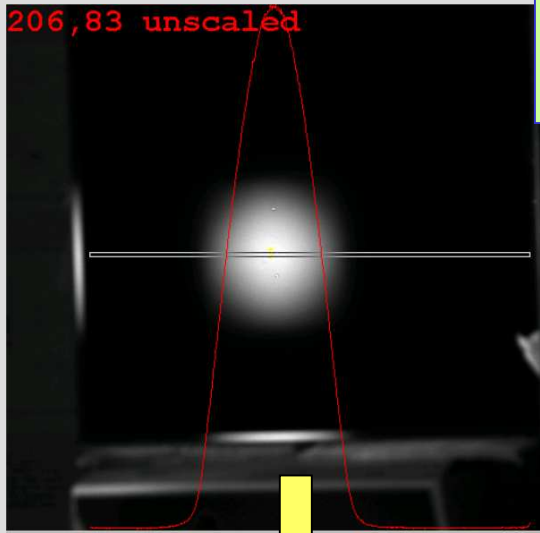


*circular*

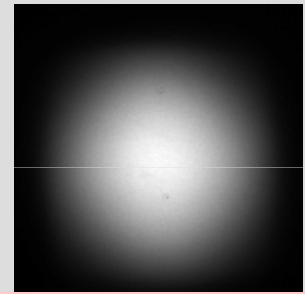
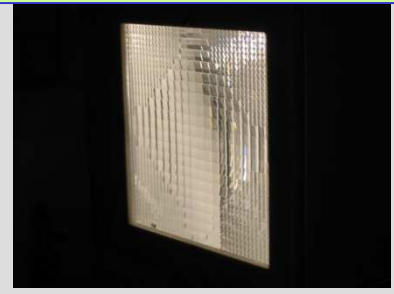
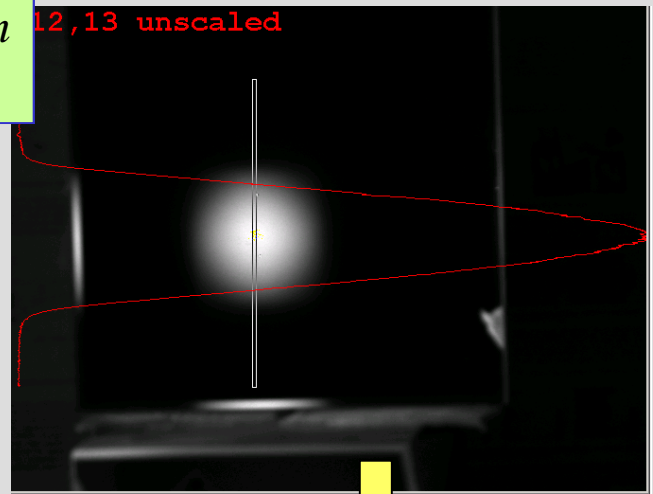
*squared*



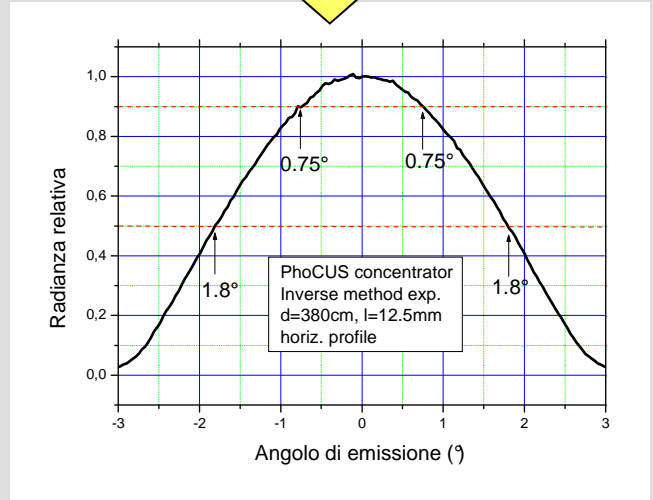
# Refract"PhoCUS" Concentrator



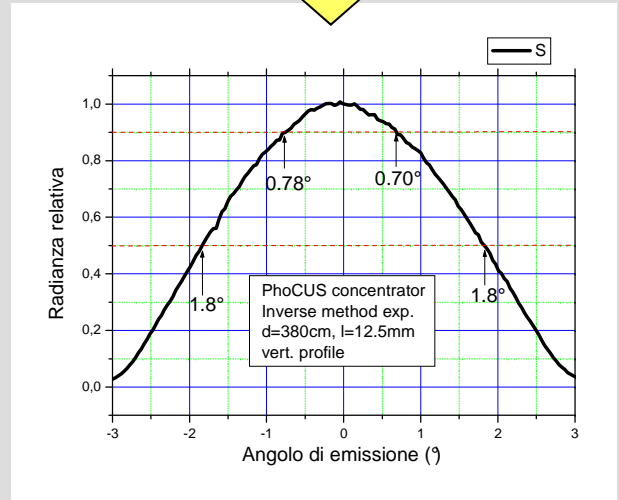
*CPC-screen distance = 380 cm*  
*Angular resolution: 1.0°*



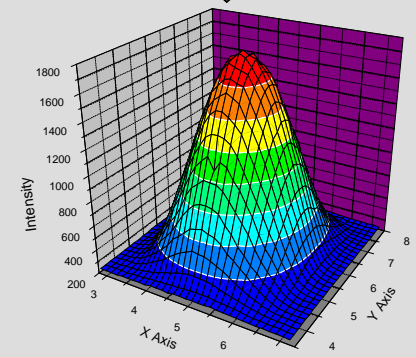
*The image on the screen*



*Horizontal profile*  
 $\theta_{acc} = 0.75^\circ / 1.8^\circ$



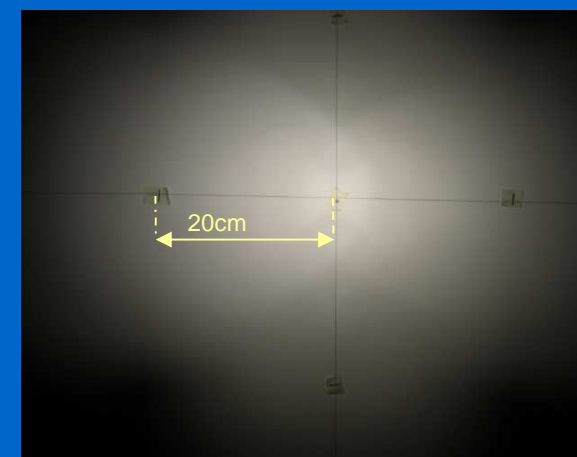
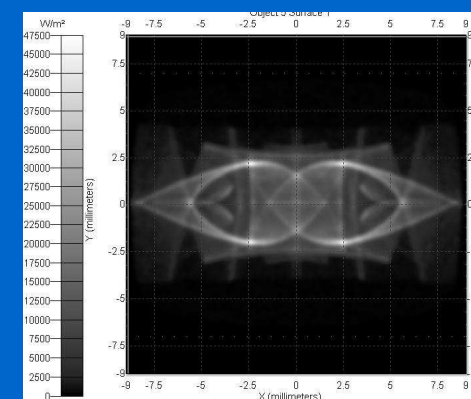
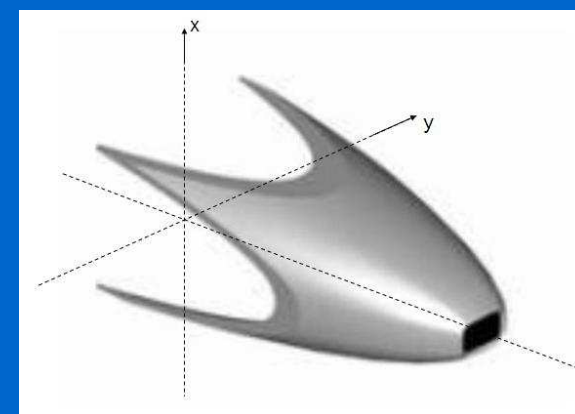
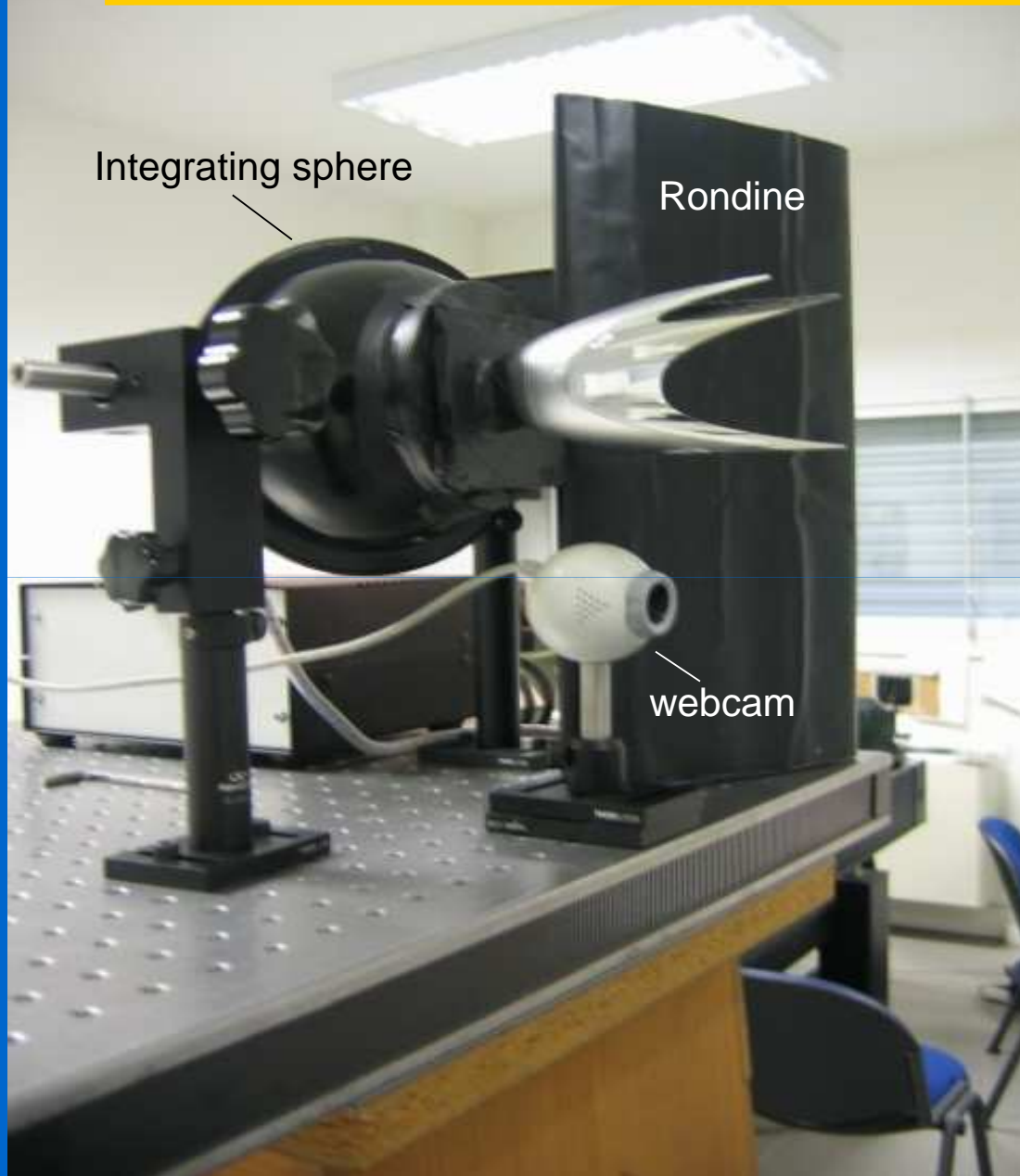
*Vertical profile*  
 $\theta_{acc} = 0.75^\circ / 1.8^\circ$



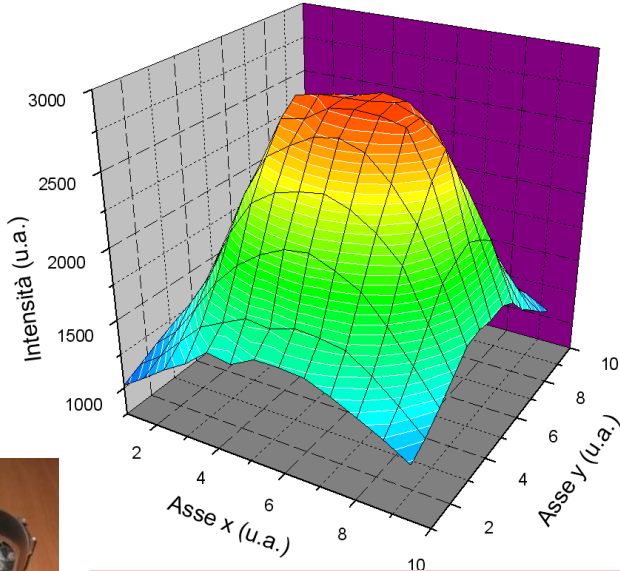
*The irradiance distribution*



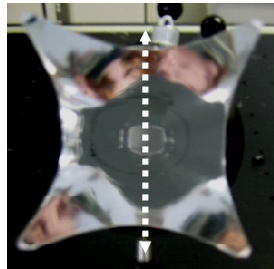
# The "Rondine" Pseudo 3D-CPC: The ILLUME set-up



# The "Rondine" Gen1 3D-CPC: Experimental results

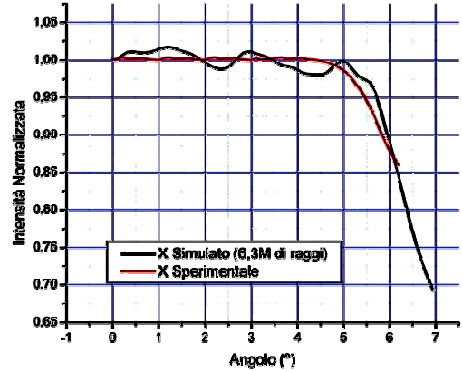
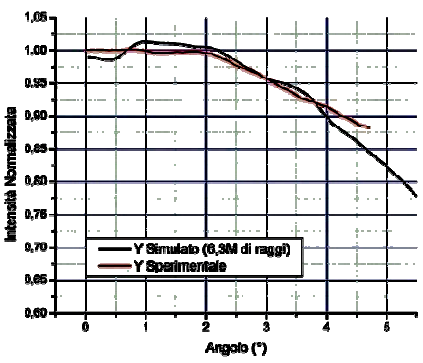


The irradiance map on the screen

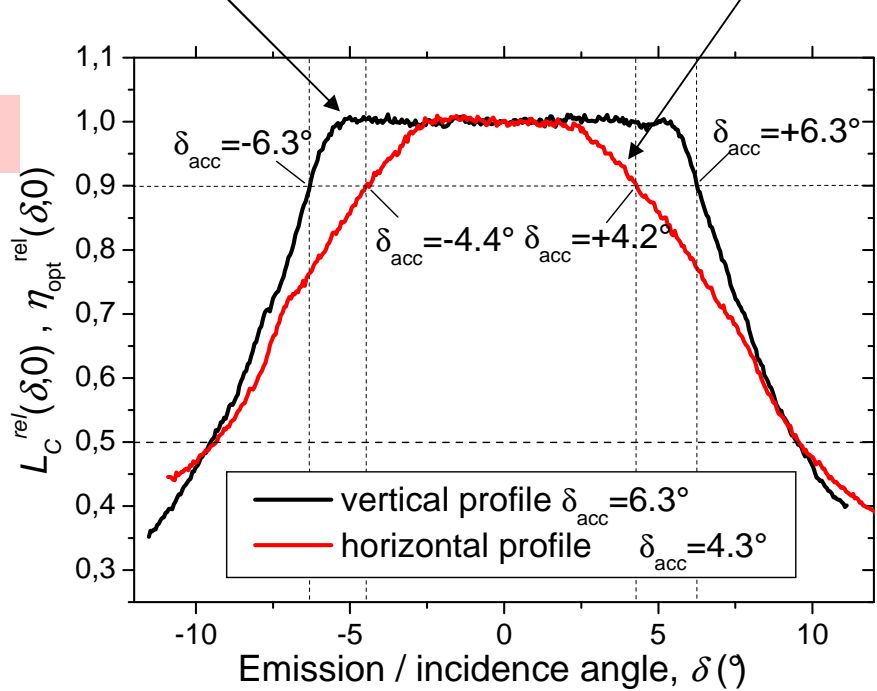


Vertical profile  
 $\theta_{acc} (90\%) \approx 6.3^\circ$

Horizontal profile  
 $\theta_{acc} (90\%) \approx 4.3^\circ$

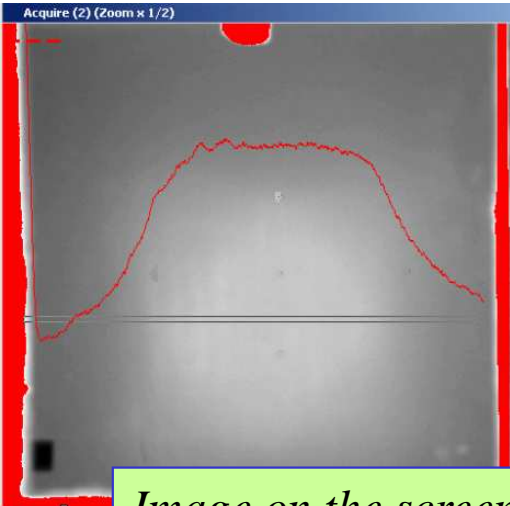


Comparison between simulations and experiments

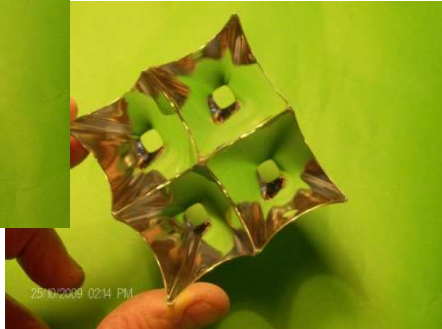


# The "Rondine" Gen2 3D-CPC: Experimental results

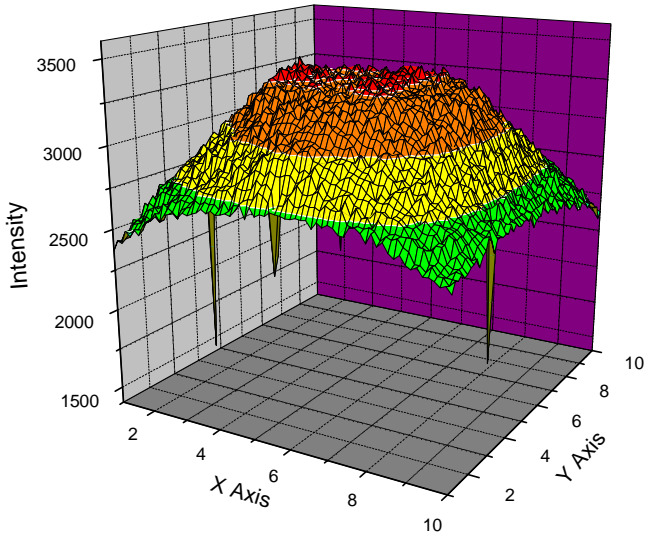
*CPC-screen distance = 229 cm*  
*Angular resolution: 0.4°*



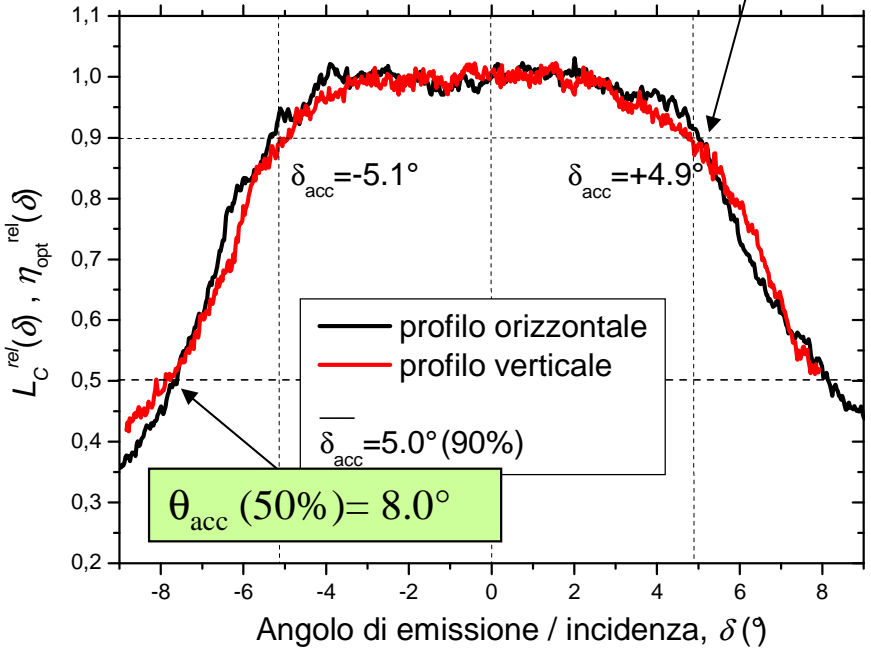
*Image on the screen*



$\theta_{acc} (90\%) = 5.0^\circ$



*Map of intensity*



## Summary of results of acceptance angles

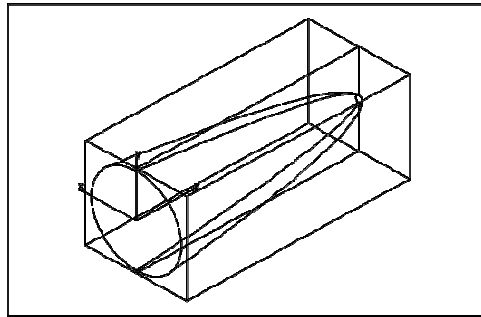
Method		Ideal 3D-CPC		TS-CPC		HT-CPC		RONDINE Gen1 Long side		RONDINE Gen1 Short side		RONDINE Gen2	
		90% Eff	50% Eff	90% Eff	50% Eff	90% Eff	50% Eff	90% Eff	50% Eff	90% Eff	50% Eff	90% Eff	50% Eff
Dir.	Sim.	4.5°	5.0°	1.3°	1.9°	4.5°	5.1°	4.3°	7.5°	5.7-6.2°	8.5°		
	Exp.			1.1° (laser)	2.8° (laser)								
Inv.	Sim.	4.5°	5.0°	1.3°	1.8°	4.5°	5.1°	4.0-4.2°	8.1°	6.0-6.1°	8.6°		
	Exp.			0.9°	2.8°			4.2-4.3°	9.5°	5.8-6.3°	9.5°	5.0°	8.0°

**Table 1.** Simulated and experimental acceptance angles for several 3D-CPCs analyzed with direct and inverse methods. Acceptance angles refer to 90% and 50% of maximum efficiency.

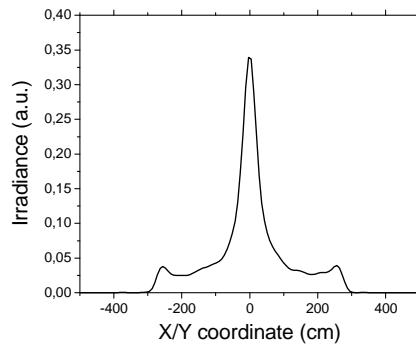
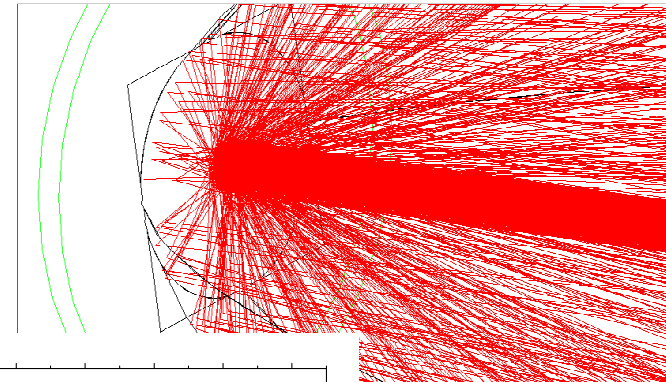
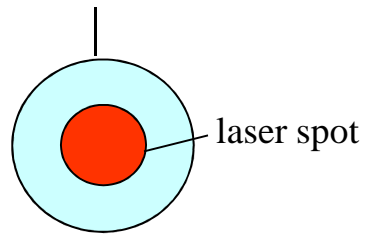
LOCAL ANALYSIS  
OF  
OPTICAL EFFICIENCY  
(BY SIMULATIONS)



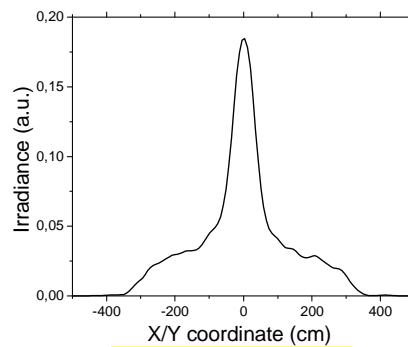
# Laser beam at the center of receiver and variable cross-section



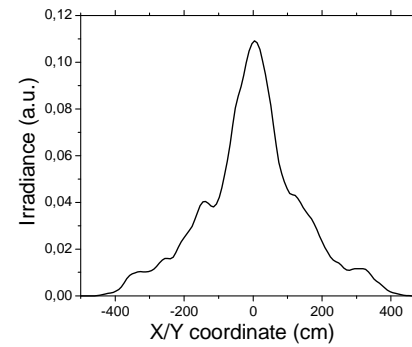
Lambertian diffuser



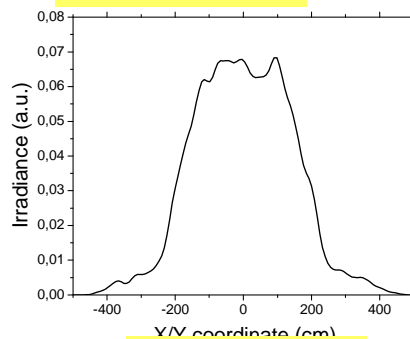
**$R= 0.05$  mm**



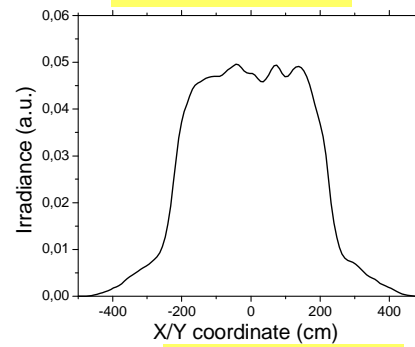
**$R= 0.5$  mm**



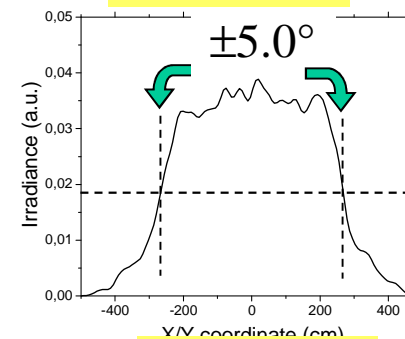
**$R= 1.0$  mm**



**$R= 2.5$  mm**



**$R= 3.5$  mm**

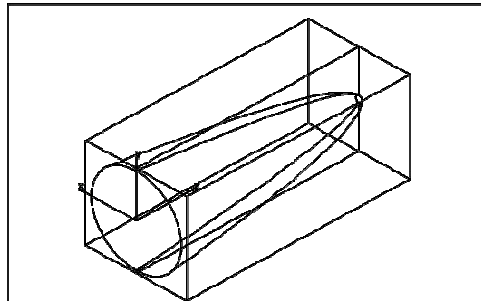


**$R= 5.0$  mm**

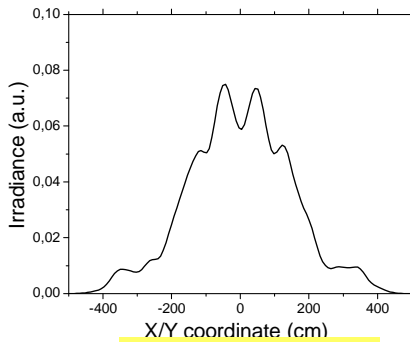
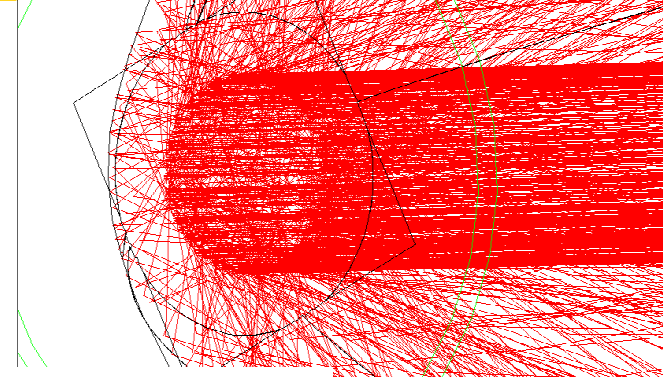
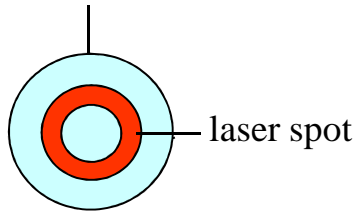
Angular interval:  
 $\pm 9.5^\circ$



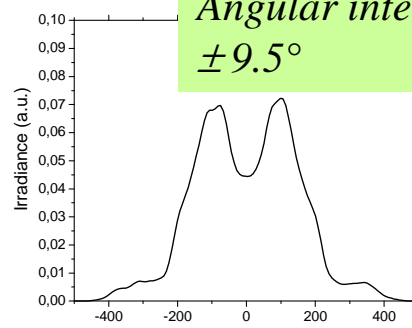
# Ring-shaped Laser beam at the center of receiver and variable internal radius (constant area = $\pi \text{ mm}^2$ )



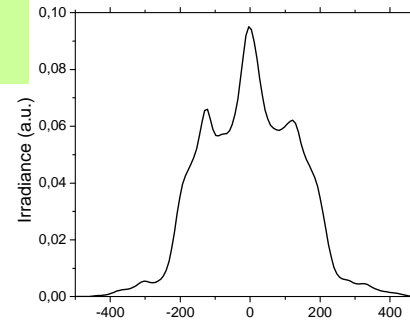
Lambertian diffuser



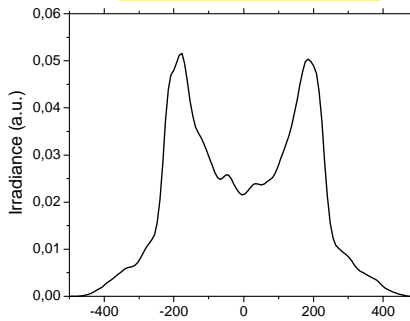
$R_{int} = 0.5 \text{ mm}$



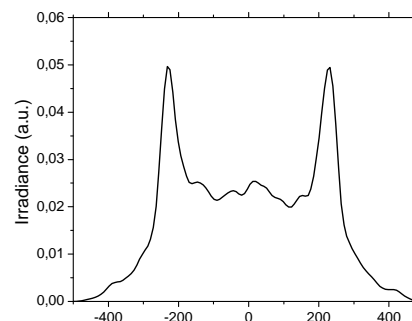
$R_{int} = 1.0 \text{ mm}$



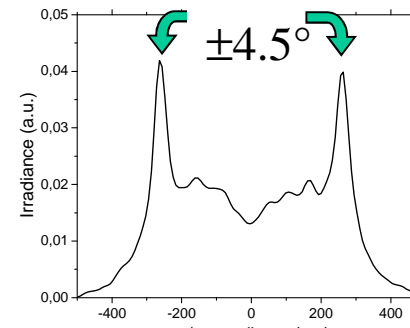
$R_{int} = 2.0 \text{ mm}$



$R_{int} = 3.0 \text{ mm}$



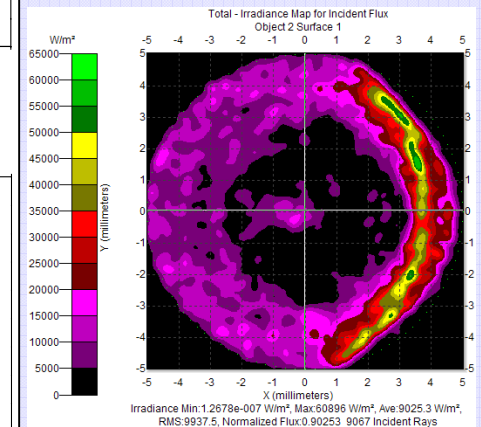
$R_{int} = 4.0 \text{ mm}$



$R_{int} = 4.9 \text{ mm}$

Angular interval:  
 $\pm 9.5^\circ$

Direct analysis



Incident beam at  $4.5^\circ$

RECENT DEVELOPMENTS  
OF “ILLUME” THEORY



## The absolute optical efficiency by ILLUME

*Until now, the inverse method furnished the relative optical efficiency*



$$\eta_{opt}(\delta, \phi) = \eta_{opt}(0) \cdot \eta_{opt}^{rel}(\delta, \phi)$$



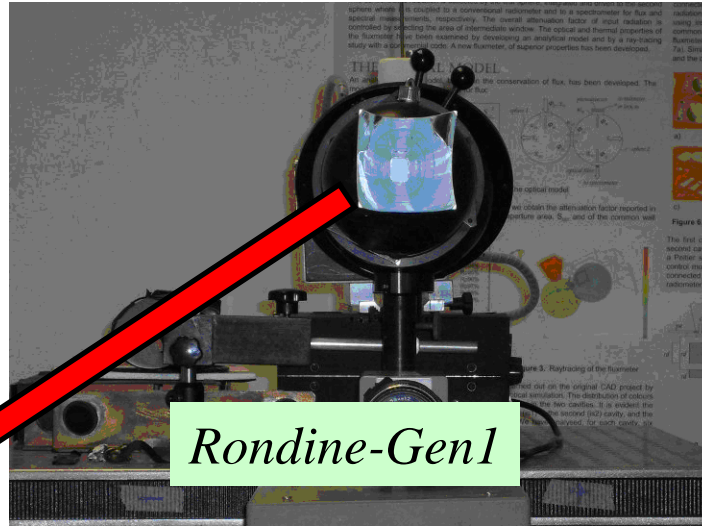
*Now we show how to obtain also the absolute efficiency at 0° incidence*

$$\eta_{opt}(0) = \frac{\bar{L}_C(0)}{L_{REC}}$$

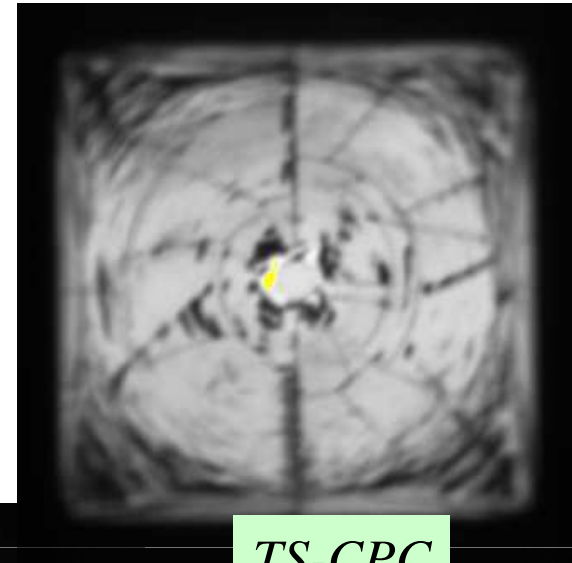
*$\bar{L}_C(0)$  is the average radiance of input aperture at 0° incidence*

*$L_{REC}$  is the (average) radiance of the receiver (Lambertian source)*

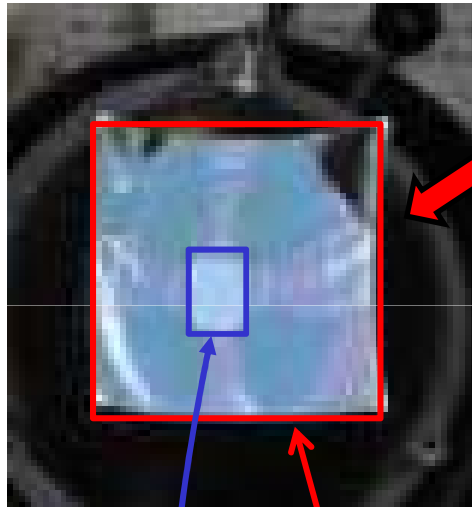
# The absolute optical efficiency by ILLUME



*Rondine-Gen1*

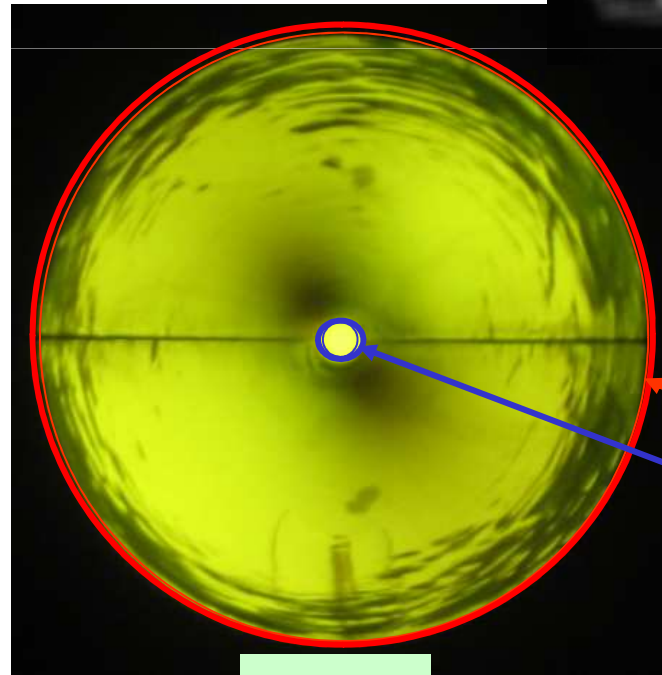


*TS-CPC*



*Rondine-Gen1*

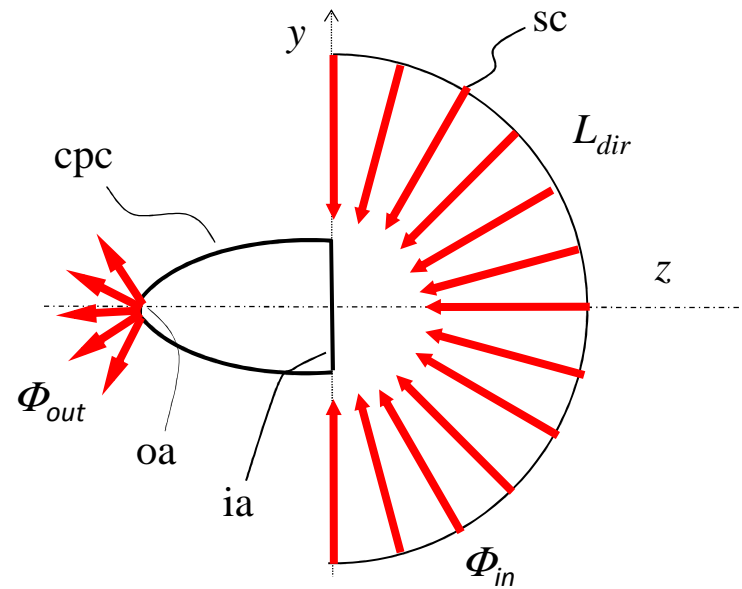
$$\frac{\bar{L}_C(0)}{L_{REC}} = \eta_{opt}(0)$$



*T-CPC*

$$\frac{\bar{L}_C(0)}{L_{REC}} = \eta_{opt}(0)$$

# THE “DIRECT INTEGRAL METHOD” (DIM)



*Overall (integral) transmission efficiency*

## DEFINITION OF NEW QUANTITIES (Integral Direct Method)

We introduce also the following new optical quantities:

$$\eta_{dir}^{int} = \frac{\Phi_{dir}^{\tau}}{\Phi_{dir}^{in}} = 2 \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \eta_{dir}(\theta) = 2 \cdot \eta_{dir}(0) \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \eta_{dir}^{rel}(\theta)$$

direct integral optical transmittance

$$\alpha_{dir}^{int} = \frac{\Phi_{dir}^{\alpha}}{\Phi_{dir}^{in}} = 2 \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \alpha(\theta) = 2 \cdot \alpha(0) \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \alpha^{rel}(\theta)$$

direct integral optical absorbance

$$\rho_{dir}^{int} = \frac{\Phi_{dir}^{\rho}}{\Phi_{dir}^{in}} = 2 \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \rho(\theta) = 2 \cdot \rho(0) \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \rho^{rel}(\theta)$$

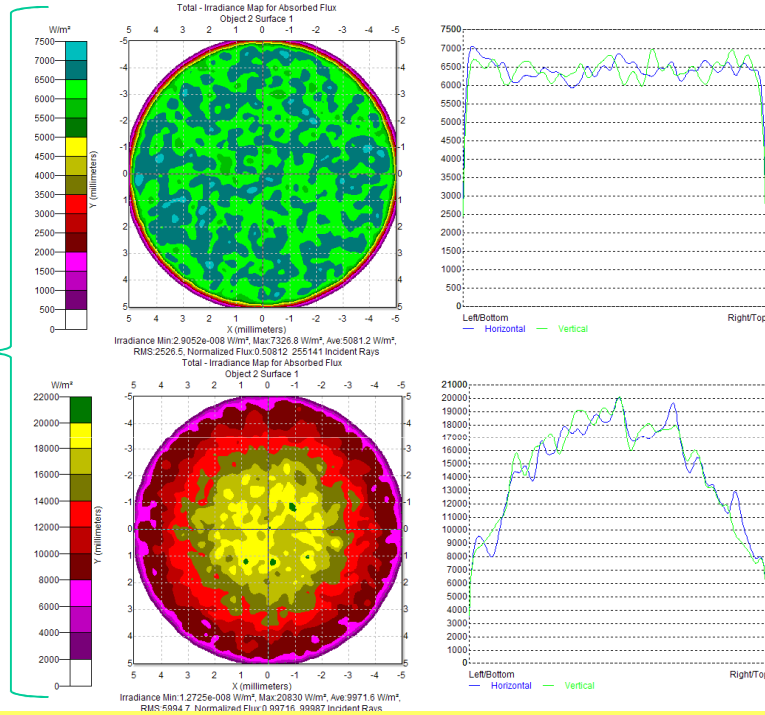
direct integral optical reflectance

Where:  $\eta_{dir}^{int} + \alpha_{dir}^{int} + \rho_{dir}^{int} = 1$

# SPATIAL DISTRIBUTION OF FLUX AT THE OUTPUT OF SC (Direct Integral Method)

**Ideal concentrator (absence of absorption):  $\alpha_{dir}(\theta_{in}, \varphi_{in}) = 0$**

$R_w = 1.0$



$\theta_{max} = 7^\circ > \theta_{acc}$

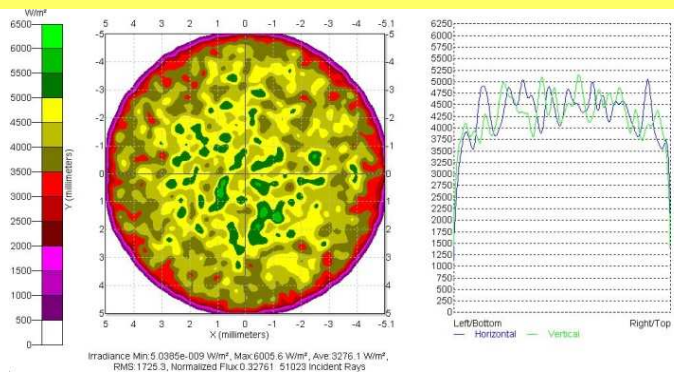
**Output flux spatially uniform !**

$\theta_{max} = 4^\circ < \theta_{acc}$

**Output flux spatially not uniform !**

**Non-ideal concentrator (absorption on the wall):  $\alpha_{dir}(\theta_{in}, \varphi_{in}) \neq 0$**

$R_w = 0.8$



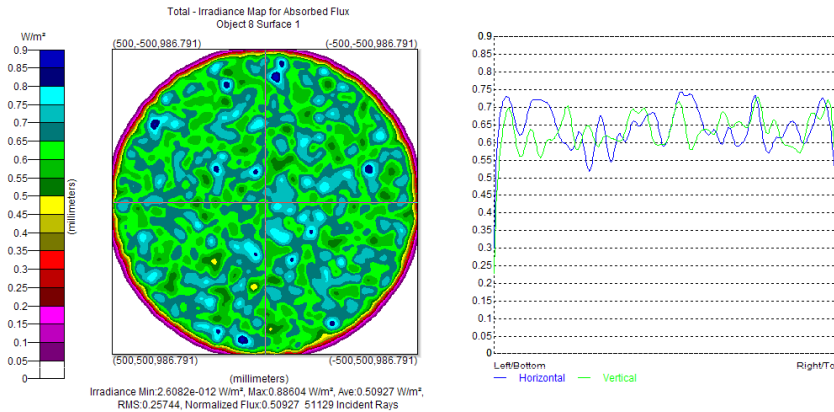
$\theta_{max} = 7^\circ > \theta_{acc}$

**Output flux spatially not uniform !**

# ANGULAR DISTRIBUTION OF FLUX AT THE OUTPUT OF SC (Direct Integral Method)

**Ideal concentrator** (absence of absorption):  $\alpha_{dir}(\theta_{in}, \varphi_{in}) = 0$

$R_w = 1.0$

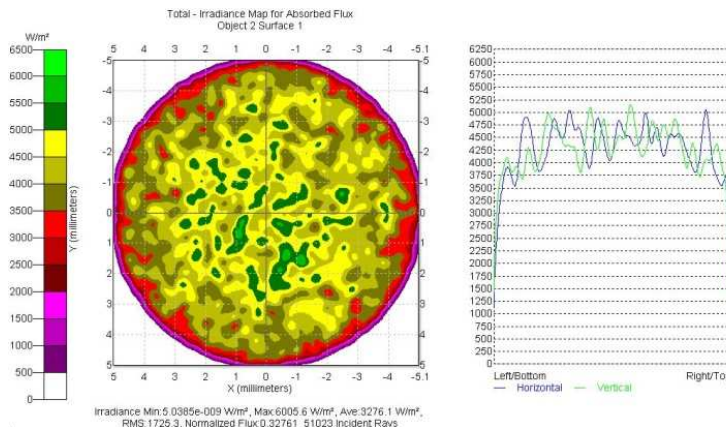


$\theta_{max} = 7^\circ > \theta_{acc}$

**Output flux Lambertian!**

**Non-ideal concentrator** (absorption on the wall):  $\alpha_{dir}(\theta_{in}, \varphi_{in}) \neq 0$

$R_w = 0.8$



$\theta_{max} = 7^\circ > \theta_{acc}$

**Output flux not Lambertian!**

## THE RADIANCE AT OUTPUT OF SC (Direct Integral Method)

Ideal concentrator (absence of absorption):  $\alpha_{dir}(\theta_{in}, \varphi_{in}) = 0$

For an **ideal concentrator** the output flux is **uniform and Lambertian**.

The **output radiance** is:

$$L_{dir}^{out} = \frac{\Phi_{dir}^{\tau}}{\pi \cdot A_{out}} = \frac{2 \cdot L_{dir}^{in} \cdot A_{in}}{A_{out}} \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \eta(\theta) =$$

$$\dots = 2 \cdot L_{dir}^{in} \cdot C_{geo} \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \eta(\theta)$$

$C_{geo}$  = geometrical concentration ratio

Non-ideal concentrator (absorption on the wall):  $\alpha_{dir}(\theta_{in}, \varphi_{in}) \neq 0$

For a **non ideal concentrator** the output flux is **non uniform and non Lambertian**.

The **average output radiance** is:

$$\bar{L}_{dir}^{out(\alpha)} = \frac{\Phi_{dir}^{\tau(\alpha)}}{\pi \cdot A_{out}} = 2 \cdot L_{dir}^{in} \cdot C_{geo} \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot \eta_{\alpha}(\theta) =$$

$$\dots = 2 \cdot L_{dir}^{in} \cdot C_{geo} \cdot \int_0^{\pi/2} d\theta \cdot \sin \theta \cdot \cos \theta \cdot [1 - \alpha(\theta) - \rho(\theta)]$$

In general we have:  $\bar{L}_{dir}^{out(\alpha)} \leq L_{dir}^{out}$

# CONCLUSIONS

We have discussed two classes of methods of characterization of solar concentrators: “direct” and “inverse”, distinguishing the way the concentrator is irradiated, if from the input or the output aperture.

The most important methods are the direct collimated method (DCM) and the inverse method (IM or ILLUME).

The DCM is largely used to obtain the transmission efficiency curve of the concentrator. It requires a lot of measurements at different angles of incidence of the collimated beam.

We have demonstrated here that also the IM method allows to obtain the same transmission efficiency curve of the concentrator.

However, we have also shown that the IM method is by far more convenient than DCM because it requires only one image to be recorded by a CCD in order to extract from it all the information about the angle-resolved optical efficiency of the concentrator.

**THANKS FOR YOUR ATTENTION !**