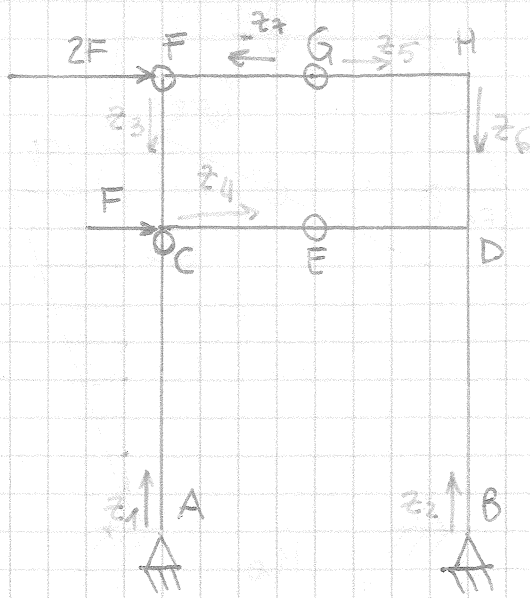
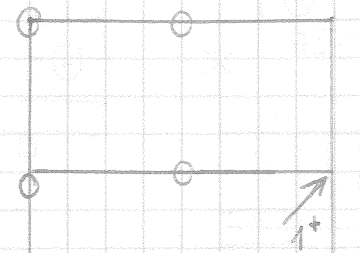
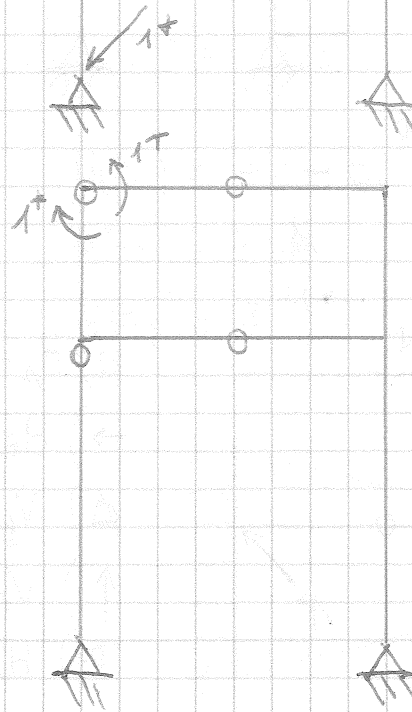




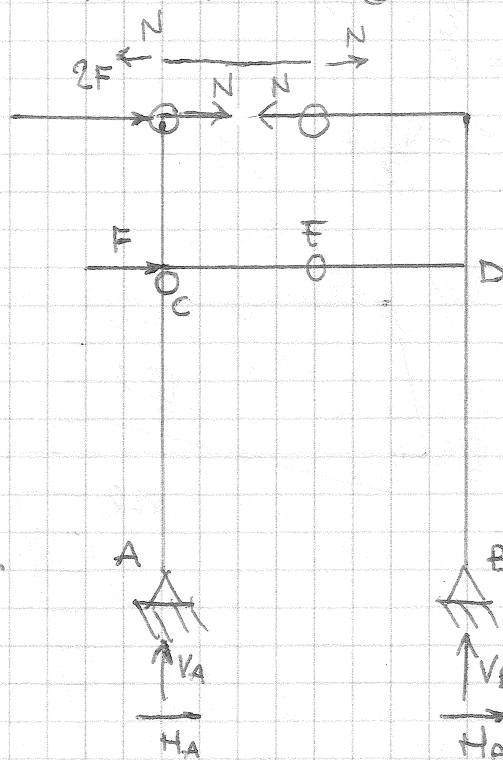
+ X_1



+ X_2



SISTEMA ○



$$E \rightarrow N \cdot l - 2F \cdot l - V_A \cdot l = 0 \quad N = 2F$$

$$C \rightarrow H_A = 0$$

$$\rightarrow H_B = -3F$$

$$B) V_A \cdot 2l + F \cdot 2l + 2F \cdot 3l = 0$$

$$V_A = -4F$$

$$1) V_A = -V_B \quad V_B = 4F$$

$$M(z_1) = 0$$

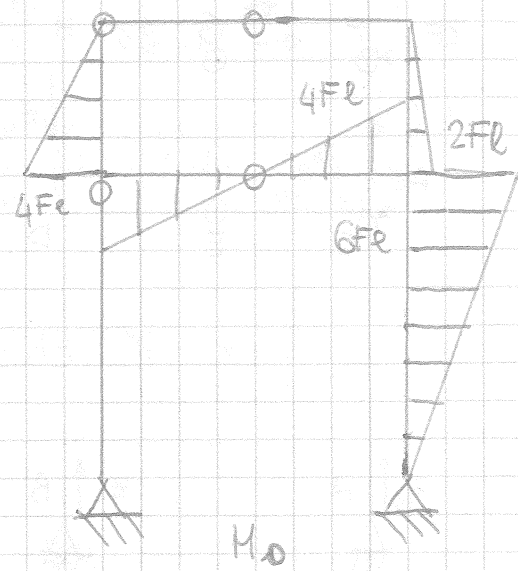
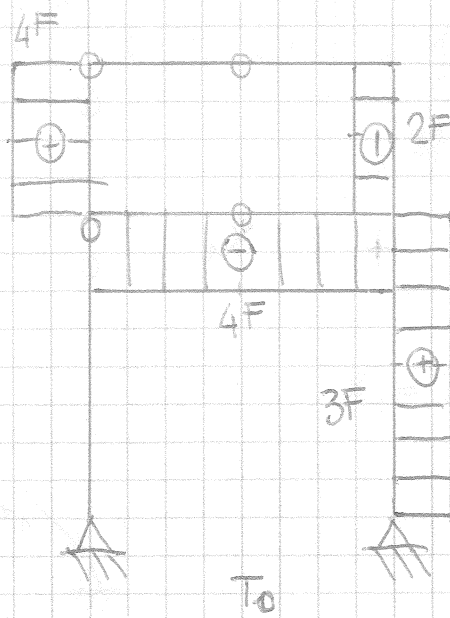
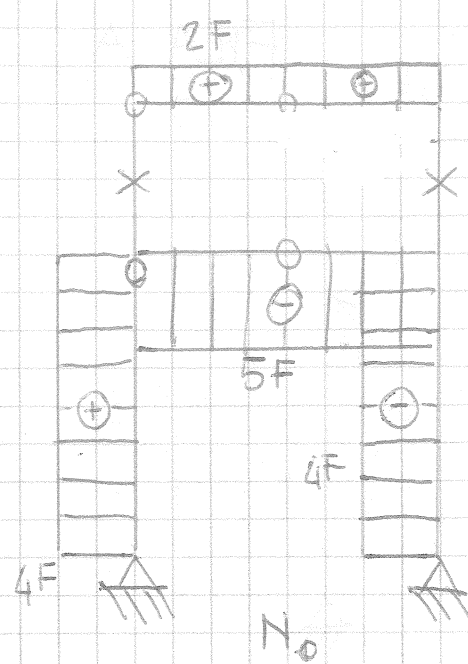
$$M(z_2) = -3Fz$$

$$M(z_3) = -4Fz$$

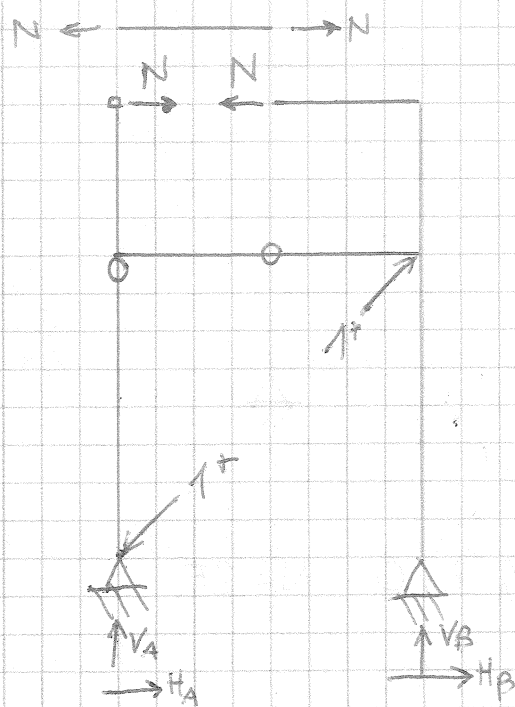
$$M(z_4) = 4Fl - 4Fz$$

$$M(z_5) = 0$$

$$M(z_6) = -2Fz$$



SISTEMA 1



$$c) H_A = \sqrt{2}/2$$

$$\rightarrow) H_B = -\sqrt{2}/2$$

$$A) V_B = 0$$

$$\uparrow) V_A = 0$$

$$\triangleright) H_A \cdot 2l - \frac{\sqrt{2}}{2} \cdot 2l + \frac{\sqrt{2}}{2} l - N \cdot l = 0$$

$$N = \sqrt{2}/2$$

$$M(z_1) = 0$$

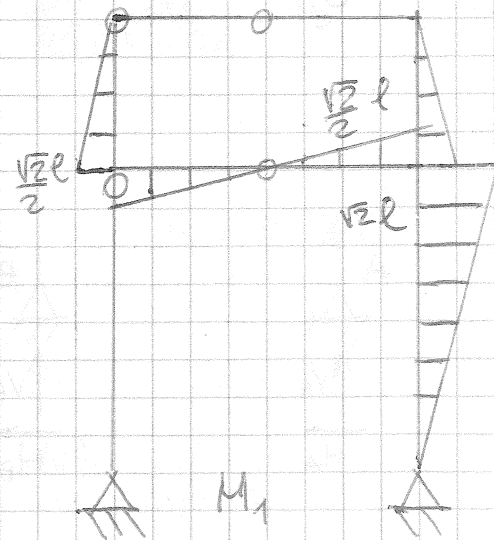
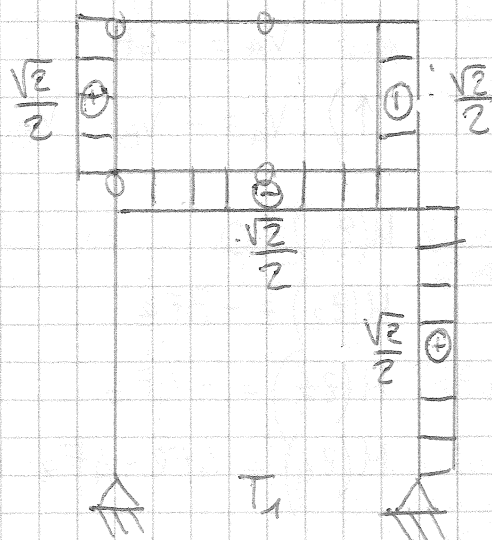
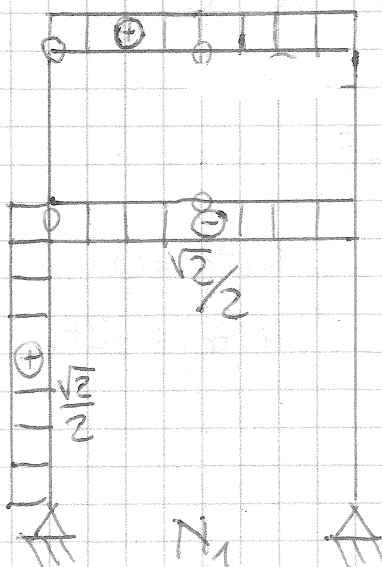
$$M(z_2) = -\frac{\sqrt{2}}{2} z$$

$$M(z_3) = -\frac{\sqrt{2}}{2} z$$

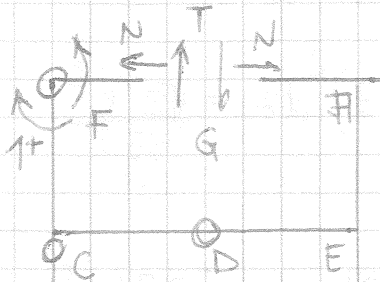
$$M(z_4) = \frac{\sqrt{2}}{2} (l - z)$$

$$M(z_5) = 0$$

$$M(z_6) = -\frac{\sqrt{2}}{2} z$$



SISTEMA 2



$$C \uparrow H_A = 0$$

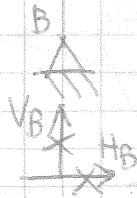
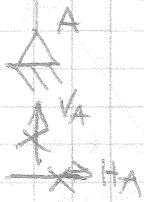
$$\rightarrow H_B = 0$$

$$C \uparrow V_B = 0$$

$$\uparrow V_A = 0$$

$$G \uparrow N = 0$$

$$F \uparrow 1 + T \cdot l = 0 \quad T = -1/l$$



$$M(z_1) = 0$$

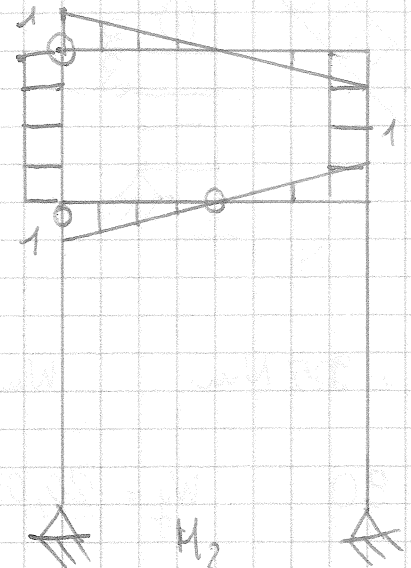
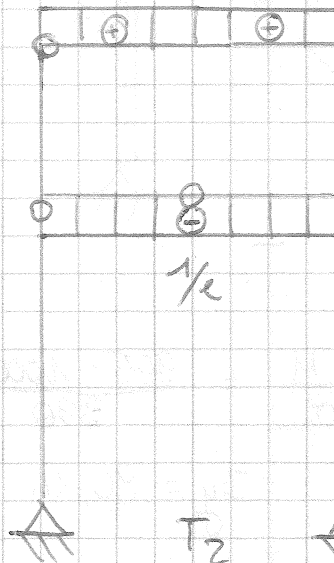
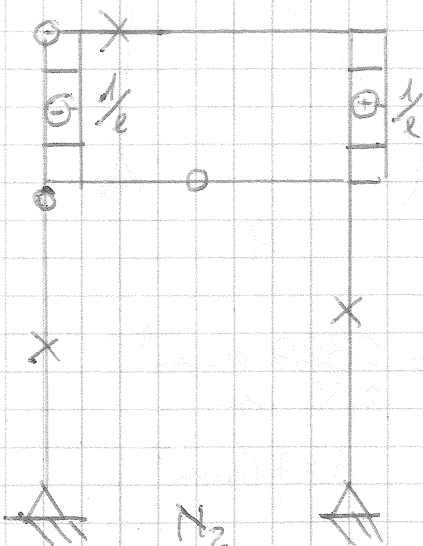
$$M(z_2) = 0$$

$$M(z_3) = -1$$

$$M(z_4) = +1 + \frac{z}{l}$$

$$M(z_5) = z/l \quad M(z_7) = -\frac{z}{l}$$

$$M(z_6) = 1$$



$$M_{10} = \frac{1}{EJ} \left[\int_0^l (-4Fz) \left(-\frac{\sqrt{2}z}{2} \right) dz + \int_0^{2l} (-3Fz) \left(-\frac{\sqrt{2}z}{2} \right) dz + \int_0^{2l} 4F \cdot \frac{\sqrt{2}}{2} \cdot (l-z)^2 dz + \int_0^l (-2Fz) \left(-\frac{\sqrt{2}z}{2} \right) dz \right] = \frac{5\sqrt{2}Fl^3}{EJ}$$

$$M_{20} = \frac{1}{EJ} \left[\int_0^l (-4Fz) (-1) dz + \int_0^{2l} (4F(l-z)) \left(1 - \frac{z}{l} \right) dz + \int_0^l (-2Fz) (1) dz \right]$$

$$= \frac{11Fl^2}{EJ}$$

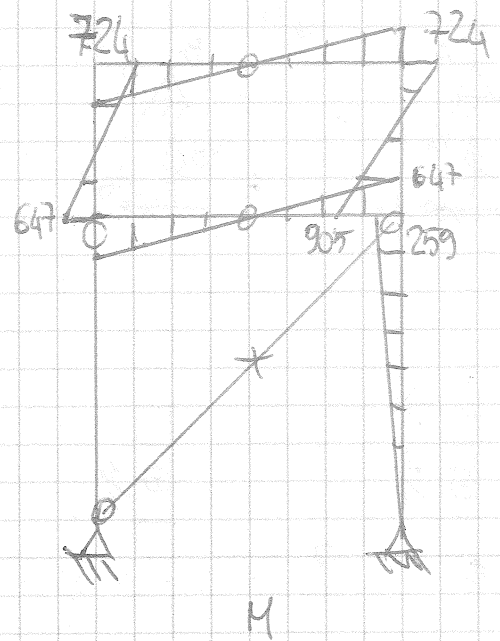
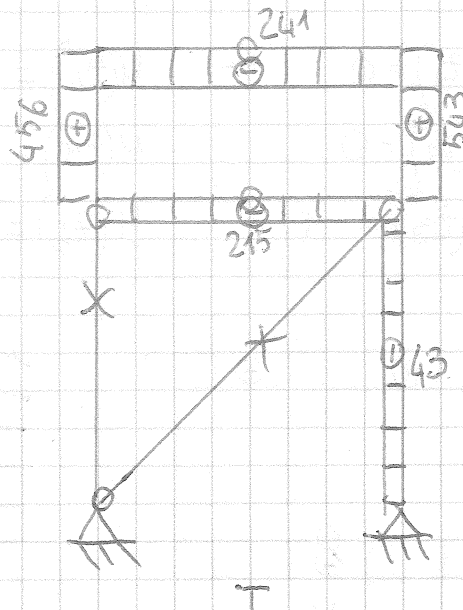
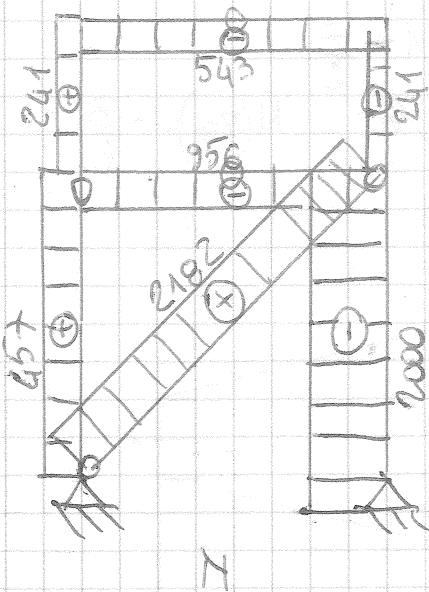
$$M_{11} = \frac{1}{EJ} \left[\int_0^{2l} \left(\frac{z^2}{2} \right) dz + 2 \int_0^l \frac{z^2}{2} dz + \int_0^{2l} \frac{1}{2} (l-z)^2 dz \right] = \frac{20l^3}{EJ}$$

$$M_{22} = \frac{1}{EJ} \left[2 \int_0^l 1 dz + 2 \int_0^{2l} \frac{(l-z)^2}{l^2} dz \right] = \frac{10l}{3EJ}$$

$$M_{12} = \frac{1}{EJ} \left[\int_0^l \left(\frac{\sqrt{2}}{2} z \right) dz + \int_0^l \left(-\frac{\sqrt{2}}{2} z \right) dz + \int_0^{2l} \frac{\sqrt{2}}{2l} (l-z)^2 dz \right] = \frac{\sqrt{2} l^2}{3EJ}$$

$$\begin{cases} M_{11} \cdot X_1 + M_{12} \cdot X_2 = -M_{10} \\ M_{12} \cdot X_1 + M_{22} \cdot X_2 = -M_{20} \end{cases}$$

$$X_1 = -2182 \text{ N} \quad X_2 = 724 \text{ Nm}$$



$$M_{max} = 905 \text{ Nm}$$

$$W_{min} = \frac{M}{\sigma_{am}} = \frac{905 \cdot 1000}{390} = 2329 \text{ mm}^3 = 2,32 \text{ cm}^3$$

IPE 80

$$W_y = 20,03 \text{ cm}^3$$

$$I_y = 80,14 \text{ cm}^4$$

$$A = 7,64 \text{ cm}^2$$

VERIFICA

$$N = 241 \text{ N}$$

$$M = 905 \text{ Nm}$$

$$\sigma = \frac{N}{A} + \frac{M}{W} = \frac{241}{7,64 \cdot 1000} + \frac{905 \cdot 1000}{20,03 \cdot 1000} = 46 < 390 \text{ MPa}$$

$$M_{11}^N = \frac{2l^3}{EJ} + \int_0^{\sqrt{2}l} \frac{1}{EA} dz = \frac{2l^3}{EJ} + \frac{\sqrt{2}l}{EA} \quad A_b = 1 \cdot 100^2$$

$$\begin{cases} M_{11}^N \cdot X_1 + M_{12} \cdot X_2 = -M_{10} \\ M_{12} \cdot X_1 + M_{22} \cdot X_2 = -M_{20} \end{cases}$$

$$X_1 = -2182 \text{ N}$$

$$X_2 = -724 \text{ Nm}$$

Tener conto della def. assiale
non cambia la risposta
strutturale